## Naturalness, Wilsonian Renormalization, and "Fundamental Parameters" in Quantum Field Theory

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#### Abstract

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In light of the increasingly strong violations of the Higgs naturalness principle revealed at the LHC, we examine the assumptions underlying one influential argument for naturalness in the sense that prohibits fine-tuning of bare Standard Model (SM) parameters. We highlight the dependence of this argument on the interpretation of these bare parameters as "fundamental parameters," by direct physical analogy with the interpretation of microscopic lattice parameters in condensed matter physics. We emphasize that while the notion of fundamental parameters is appropriate to some applications in condensed matter physics, it plays no essential role in the effective field theories (EFT's) of high-energy physics. We distinguish two ways of understanding high-energy EFT's within the Wilsonian framework, the first of which takes an EFT to be uniquely defined by a single set of physical, fundamental bare parameters, and the second of which dispenses entirely with the notion of fundamental parameters. In this latter view, an EFT is instead defined by a one-parameter class of physically equivalent parametrizations related by Wilsonian renormalization group flows. From this perspective, the delicate cancellation between bare Higgs mass and quantum corrections appears as an eliminable artifact of mathematical convention, rather than as a physical coincidence calling out for explanation by a deeper theory. Thus, we aim to clarify the distinction between two physical interpretations of Wilsonian EFT's and bare parameters in high energy physics, and to show in light of this distinction how one formulation of the naturalness requirement, based on the notion that bare parameters at an EFT's physical cutoff constitute "fundamental parameters," may be rooted in an excessively literal reading of the high-energy/condensed-matter analogy.

#### 1 Introduction

The naturalness principle has served as an extremely influential guide to model building in high-energy physics for the past several decades, notably functioning as the basis for theoretical arguments in favor of supersymmetry, and for the expectation of discovering signatures of Beyond the Standard Model (BSM) physics at the Large Hadron Collider (LHC). The principle has been formulated variously as a prohibition against "unlikely" finetuning of Standard Model (SM) parameters, a prohibition on delicate sensitivity between physics at different energy scales, and as the requirement that all dimensionless parameters in an effective field theory be of order one unless protected by a symmetry. The continuing absence of BSM physics up to ever higher energies, combined with the notorious quadratic dependence of the physical Higgs mass on heavy scales, entails increasingly strong violations of naturalness in all of these formulations (suitably interpreted). There remains an important open question concerning what to make of this fact. Should failure of naturalness be regarded as posing an especially urgent demand for explanation of the Higgs mass over other SM parameters? Should failure of naturalness be accepted as a brute fact, so that we simply forgo demand for such further explanation? Or should the Higgs naturalness principle itself be abandoned, and specifically the notion that the quadratic sensitivities of the Higgs mass pose a special problem not posed by other Standard Model parameters?

In favor of the first view, that failure of naturalness remains a special puzzle to be resolved by BSM theories, Giudice writes, "If the LHC rules out dynamical solutions to Higgs naturalness at the weak scale, it does not eradicate the problem: a doctor who is unable to find the right diagnosis cannot simply declare the patient healed. Even in post-natural times, the concept of naturalness cannot simply be ignored ... One way or another, naturalness will still play a role in the post-naturalness era" (Giudice, 2017). Thus, on Giudice's view, although we are entering a "post-naturalness" era, failure of Higgs naturalness remains as much a problem as ever. On the other hand, several voices have urged abandonment of the naturalness principle itself - at least, as it has been applied in the cases of the Higgs and of the cosmological constant, which are closely analogous (Woit, 2014), (Hossenfelder). Since our discussion below inclines toward this latter point of view, we wish to acknowledge at the outset that from one perspective, it may seem all too easy, now that failure of naturalness in the Standard Model has been increasingly empirically confirmed, to join the chorus of voices decrying naturalness. However, we emphasize that the status of the naturalness principle itself is far from settled by existing evidence: violation of naturalness by the Standard Model <sup>1</sup> does not in and of itself imply that the fault lies with the naturalness principle since it may be the case, as Giudice suggests, that the fault instead lies with the Standard Model description of the Higgs.

Nevertheless, failure of predictions for new physics at the LHC based on naturalness motivates careful re-examination of the arguments that have been advanced in support of the naturalness principle. Here, we probe a possible point of weakness in one specific but highly influential rationale for naturalness in the sense that precludes "unlikely" or "contrived" tuning of the Standard Model's bare parameters at its physical cutoff scale.<sup>2</sup> We show how this rationale, advanced by some of the original advocates of the naturalness principle, is grounded in the physical interpretation of bare parameters at a Wilsonian effective field theory's physical cutoff as "fundamental parameters," by analogy with the physical, microscopic lattice parameters that are employed in certain condensed matter models. We argue that in the Wilsonian approach to the non-perturbative definition of EFT's, based on assuming finite values for the cutoff and bare parameters, the notion that there exists a single, physically preferred set of fundamental parameters functions as an idle metaphysical supposition in generating the EFT's successful empirical predictions. Moreover, this assumption is not necessary to ensure that all quantities calculated in the EFT are finite and mathematically well-defined. Instead, we argue, one may interpret the formalism of Wilsonian renormalization without assuming the existence of a single physically preferred bare parametrization, instead understanding an EFT to be defined by a one-parameter class of physically equivalent parametrizations that describe one and the same set of physical amplitudes, where no single parametrization is regarded as more "physical" or "fundamental" than any other. We argue that in the absence of fundamental parameters, the delicate cancellation between bare Higgs mass and quantum corrections thought to produce the naturalness problem may be regarded as an eliminable artifact of mathematical convention. This undermines the notion that such cancellations depend on cosmically unlikely coincidences, and that the value of the bare Higgs mass therefore stands in more urgent need of explanation by BSM theories than do other SM parameters. From this perspective, the notion that a high-energy EFT's bare parameters at its physical cutoff constitute "fundamental parameters" appears to be rooted in an excessively literal, excessively "physical" interpretation of the analogy between high-energy and condensed matter field theories.<sup>3</sup> To make this point, we employ Doreen

<sup>&</sup>lt;sup>1</sup>As is sometimes noted, there is no sharp division between "natural" and "unnatural" theories; naturalness is a matter of degree, often associated with the degree of fine tuning or sensitivity to a theory's "fundamental parameters." Thus, it is to some a degree a matter of taste at precisely what point one takes the SM to have violated the naturalness criterion.

<sup>&</sup>lt;sup>2</sup>In this discussion, we do not explicitly address alternative formulations of the naturalness criterion, such as those that preclude delicate sensitivity between physics at different scales, and those that require dimensionless parameters to be of order one. For extended philosophical analysis of naturalness in the first sense, see Williams' (Williams, 2015); for a physicist's perspective on naturalness in this sense, see Giudice's (Giudice, 2013). For discussion of naturalness in the second sense, see for example the original article by 't Hooft, ('t Hooft, 1980), and Wells' (Wells, 2015).

<sup>&</sup>lt;sup>3</sup>By "high-energy EFT," we mean to designate an EFT used in the description of elementary particles,

Fraser's distinction between "formal" and "physical" analogies in physics, and build on her use of this distinction in the specific context of the high-energy/condensed-matter analogy.

Our discussion is outlined as follows. Section 2 establishes several foundational assumptions about the formal definition of Wilsonian effective field theories that will serve to ground our later discussion of naturalness. Section 3 introduces the formulation of the Higgs naturalness problem as arising from the need for a delicate cancellation between the bare Higgs mass and its quantum corrections, and introduces two conflicting views of this cancellation: the first view takes this cancellation as an instance of mysterious fine tuning, while the other adopts a more deflationary interpretation. Section 4 reviews the historical motivations for imposing naturalness cited by original proponents of the naturalness principle, underscoring the reliance of these formulations on the notion of "fundamental parameters." We attempt to state explicitly the core features of the interpretation of Wilsonian EFT's based on fundamental parameters, and consider the status of Higgs fine tuning from this perspective. In Section 5, we review D. Fraser's distinction between "formal" and "physical" analogies, and specifically between "formal" and "physical" interpretations of the HEP/CMP analogy, which provides a useful characterization of the distinction between the two views of Wilsonian EFT's considered here. Section 6 clarifies one interpretation of Wilsonian EFT's in the absence of fundamental parameters, highlighting the main points of contrast with interpretations based on fundamental parameters, and offering several arguments in support of this alternative view. We conclude that in the absence of fundamental parameters, Higgs fine tuning is an eliminable artifact associated with one conventional choice of bare parametrization, rather than a physical coincidence urgently demanding explanation by deeper theories. Section 7 is the Conclusion.

## 2 Foundational Assumptions

How is a quantum field theory mathematically defined? This is a notoriously difficult and controversial question, with the difficulties resulting in large part as a consequence of the infinities that occur in perturbative expansions of QFT amplitudes. There exist multiple rival research programs, including the algebraic and constructive approaches to quantum field theory, that have attempted in different ways to place QFT on firm mathematical foundations. However, continuum approaches such as the algebraic approach are only known to work in contrived and unphysical settings - for example, which the number of space-time dimensions is less than four - and thus far have had difficulty incorporating any of the physically realistic QFT's, such as the Standard Model or quantum electrodynamics, used to describe the phenomenology observed in accelerators like the LHC. Largely for this reason, we adopt the alternative strategy based on Wilson's effective field theory approach to renormalization and quantum field theory, which takes quantum field theories such as the Standard Model and quantum electrodynamics to be defined with a finite cutoff, and thereby avoids the problematic infinities that occur in continuum approaches. <sup>4</sup>

rather than an EFT employed in the description of condensed matter systems. Thus, on this usage, a "high-energy EFT" may also describe the behavior of elementary particles at low energies.

<sup>&</sup>lt;sup>4</sup>The virtues and shortcomings of such a cutoff-based approach, as contrasted with axiomatic, continuumbased approaches such as algebraic quantum field theory (AQFT) and constructive field theory, have been debated extensively by Wallace and Fraser in (Wallace, 2006), (Wallace, 2011), (Fraser, 2009), (Fraser, 2011). Largely for the reasons articulated by Wallace - in particular, the difficulty in axiomatic approaches of making contact with the empirical success of the Standard Model - we choose to ground our discussion in a Wilsonian cutoff-based rather than an axiomatic approach to the formulation of quantum field theory.

Beyond the infinities that occur in perturbative expansions, there is the closely related problem of how to define a quantum field theory outside the context of perturbation theory. Such problems are especially salient in the context of low-energy QCD calculations, where perturbation theory breaks down. To address both problems, the Wilsonian strategy of defining a QFT with a finite cutoff is often employed; see for example (Collins, 1984) and (Montvay and Münster, 1997). As is often emphasized, this strategy permits one to numerically define the amplitudes of a QFT in a way that is completely finite and does not rely on the assumption of small coupling; perturbative expansions are then understood as generating approximations to these non-perturbatively defined quantities. In our discussion of naturalness below, we likewise understand QFT's to be non-perturbatively defined in this manner. Since QFT's so defined are generally understood to be empirically valid only up to some finite physical cutoff scale  $\Lambda_{phys}$ , they are often designated as "effective field theories" (EFT's). However, as we discuss in later sections, there are at least two distinct ways of interpreting the Wilsonian formalism, one based on the assumption that there exists a set of "fundamental parameters" that serve to uniquely define the theory, and another that treats different finite parametrizations on equal footing.

#### 2.1 Cutoff-Based Approach to Defining Effective Quantum Field Theories

The most common approach to the non-perturbative definition of EFTs starts from the Feynman path integral, then deriving correlation functions, S-matrix elements, pole masses and other physical quantities from these; see, e.g. (Montvay and Münster, 1997). <sup>6</sup> The path integral is mathematically defined via imposition of a cutoff regulator (e.g., hard momentum cutoff, smooth momentum cutoff, real space lattice) and Wick rotation to Euclidean space-time. Adopting a lattice spacing a for concreteness - which imposes an effective momentum cutoff of order  $\frac{2\pi}{a}$  - the path integral  $\mathcal{Z}[J]$  for a theory with Lagrangian  $\mathcal{L}(x)$  in the presence of a classical external source field J(x) is

$$\mathcal{Z}[J] = \int^{\Lambda} \mathcal{D}\phi \ e^{i \int d^4 x [\mathcal{L}(\phi(x)) + J(x)\phi(x)]}$$

$$\equiv \int \prod_{i=1}^{M} d\phi_i \ e^{ia^4 \sum_{i=1}^{M} [\mathcal{L}(\phi_i) + J_i\phi_i]},$$
(1)

where  $\mathcal{L}(\phi(x))$  is the "bare" Lagrangian of the theory,  $M = (\lfloor L/a \rfloor)^4$ , *a* is the lattice spacing on a hypercubic 4-D lattice (note that the time dimension has now been discretized as well), *L* is the length of each edge of the lattice,  $J_i \equiv J(x_i)$  is a background source field,  $\phi_i \equiv \phi(x_i)$ , and  $x_i \equiv (n_0 a, n_1 a, n_2 a, n_3 a)$  for  $n_\alpha \in \mathbb{Z}$  and  $-\frac{L}{2a} \leq n_\alpha \leq \frac{L}{2a}$ ,  $\alpha = 0, 1, 2, 3$ . The lengths *a* and *L* function, respectively, as a UV regulator associated with an upper momentum cutoff

For technical discussion of constructive approaches to defining QFT on the continuum, see for example (Rivasseau, 2014). For philosophical discussion of constructive QFT see Hancox-Li (Hancox-Li, 2017).

<sup>&</sup>lt;sup>5</sup>For philosophical analysis of approaches to the foundations of QFT based on perturbation theory, see, for example, the recent work of Miller and J. Fraser (Miller, 2016), (Fraser, 2017).

<sup>&</sup>lt;sup>6</sup>The correlation functions of a quantum field theory contain sufficient information to reconstruct the field dynamics and entire Hilbert space of the theory; this result is encoded formally in the Wightman Reconstruction Theorem; see (Streater and Wightman, 2016), Ch. 3. Since this theorem is proven in the context of axiomatic formulations of QFT, it is possible that significant work remains to be done in determining whether and how it can be modified to accommodate EFT's defined in the Wilsonian framework.

of  $\Lambda = \frac{2\pi}{a}$  and an IR regulator associated with lower momentum cutoff  $\frac{2\pi}{L}$ . <sup>7</sup>

In keeping with the Wilsonian approach, the bare Lagrangian  $\mathcal{L}$  is taken to consist of all terms consistent with a given choice of fields  $\phi$  and symmetries:

$$\mathcal{L} = \sum_{n} g_{n} \mathcal{O}_{n}$$
  
=  $g_{1} \left(\partial_{\mu}\phi\right)^{2} + g_{2}\phi^{2} + g_{3}\phi^{4} + g_{4}\phi^{6} + g_{5}(\partial_{\mu}\phi)^{2}\phi^{2} + g_{6}\phi^{8} + \dots,$  (2)

where the bare parameters  $g_i$  can be any real numbers. Here, we use the term "bare" to refer to any parametrization of the theory of the form given by the path integral (1) and Lagrangian (2); that is, a "bare" parameter on our usage is a parameter appearing in the Lagrangian of the path integral, whatever the chosen value of  $\Lambda$ . <sup>8</sup> The calculation of physical quantities such as pole masses and cross sections from  $\mathcal{Z}[J]$  is mediated via the calculation of *n*-point Green's functions  $G^{(n)}(x_1,...,x_n)$ , which encode the full dynamics of the QFT:

$$G^{(n)}(x_1, ..., x_n) \equiv \frac{\int^{\Lambda} \mathcal{D}\phi \ \phi(x_1) \ ... \ \phi(x_n) \ e^{i \int d^4 x \sum_n g_n \mathcal{O}_n}}{\int^{\Lambda} \mathcal{D}\phi \ e^{i \int d^4 x \sum_n g_n \mathcal{O}_n}}$$
(3)  
$$= \frac{(-i)^n}{\mathcal{Z}[0]} \frac{\delta^n}{\delta J(x_1) \ ... \ \delta J(x_n)} \bigg|_{J=0} \mathcal{Z}[J].$$

For example, the physical or "pole" mass  $m_p$  is calculated from the bare parameters as the lowest-lying pole of the Fourier transform of the two-point function,

$$G^{(2)}(x_1, x_2) = \int^{\Lambda} \frac{d^4 p}{(2\pi)^4} e^{ip(x_1 - x_2)} \left[ \frac{iZ(g, \Lambda)}{p^2 - m_p^2(g, \Lambda)} + \int_{\sim 4m_p^2}^{\Lambda} d\mu \, \frac{\rho(\mu)}{p^2 - \mu^2} \right], \tag{4}$$

where  $\rho(\mu)$  is the so-called spectral density function,  $g \equiv (g_1, g_2, g_3, ...)$ ; the symbol ~ in the lower limit ~  $4m_p^2$  of the second integral is intended to signal the possibility of bound states below the threshold energy-squared for multi-particle production  $(2m_p)^2$ . The field renormalization  $Z(g, \Lambda)$  is defined as  $Z(g, \Lambda) \equiv |\langle \lambda(0) | \hat{\phi}(0) | \Omega \rangle|^2$ , where  $|\lambda(0)\rangle$  is a oneparticle energy eigenstate of the full interacting theory with zero spatial momentum. The S-matrix element for  $2 \rightarrow n-2$  particle scattering can be calculated from Green's functions via the LSZ reduction formula:

$$S(p_1, ..., p_n; g, \Lambda) = \tilde{G}^{(n)}(p_1, ..., p_n; g, \Lambda) \quad \tilde{G}^{(2), -1}(p_1; g, \Lambda) ... \tilde{G}^{(2), -1}(p_n; g, \Lambda).$$
(5)

<sup>&</sup>lt;sup>7</sup>For the purposes of our discussion, only the UV regulator a will be relevant; the IR regulator L will not play a role.

<sup>&</sup>lt;sup>8</sup>We should acknowledge here a distinct use of the term "bare" within the context of Wilsonian renormalization, in which it is only the path integral parametrization for some *particular* choice of cutoff  $\Lambda_0$ , associated with the physical cutoff scale of the theory, that constitutes the "bare" parametrization. Parametrizations related to this parametrization via Wilsonian RG transformations are designated as "renormalized." This usage reflects the presence in statistical mechanical or condensed matter applications of a sharply defined physical cutoff and bare parameters associated associated with a real physical lattice. By contrast, the usage of "bare" employed here, in which bare parameters absorb the  $\Lambda$  dependence of Z[J] without being attached to any particular value of  $\Lambda$ , is consistent with perturbative renormalization schemes in which the bare parameters likewise depend on  $\Lambda$ , without being uniquely attached to any single finite value of  $\Lambda$ .

This in turn can be used to infer the differential and total cross section of the process in question. Note that the above relations are non-perturbative, and that all quantities defined are finite and in principle calculable from first principles.

#### 2.2 The Wilsonian Renormalization Group

The Wilsonian renormalization group (RG) consists is a set of transformations on the parameters g and  $\Lambda$  of Z[J], that leave the value of Z[J] exactly unchanged. From this it follows that the values of physical quantities such as pole masses and (mod-squared) S-matrix elements computed from Z[J] remain exactly unchanged under these transformations. <sup>9</sup> Thus, the Wilsonian RG determines the cutoff dependence  $g(\Lambda)$  that must be ascribed to bare Lagrangian parameters g in order that Z[J] remain invariant. The process of transforming from a bare parametrization ( $g(\Lambda), \Lambda$ ) at one cutoff scale to another bare parametrization ( $g(\Lambda'), \Lambda'$ ) at a slightly lower cutoff scale is implemented by splitting the path integral into an integration over field modes  $\phi_{\Lambda'}$  with momenta less than or equal to some lowered cutoff  $\Lambda' = \Lambda - \delta\Lambda$ , and an integration over field modes  $\phi_{\delta\Lambda} = \phi_{\Lambda} - \phi_{\Lambda'}$  with momenta greater than  $\Lambda'$  but less than  $\Lambda$ , and then explicitly performing the latter integral:

$$\mathcal{Z}[0] = \int \mathcal{D}\phi_{\Lambda} \ e^{i\int d^{4}x \ \mathcal{L}(\phi_{\Lambda};g(\Lambda))}$$
  
=  $\int \mathcal{D}\phi_{\Lambda'} \left( \int \mathcal{D}\phi_{\delta\Lambda} e^{i\int d^{4}x \ \mathcal{L}(\phi_{\Lambda} + \phi_{\delta\Lambda};g(\Lambda))} \right)$   
=  $\int \mathcal{D}\phi_{\Lambda'} e^{i\int d^{4}x \ \mathcal{L}(\phi_{\Lambda'};g(\Lambda'))}$  (6)

where  $e^{i\int d^4x \ \mathcal{L}(\phi_{\Lambda'};g(\Lambda'))} \equiv \int \mathcal{D}\phi_{\delta\Lambda} e^{i\int d^4x \ \mathcal{L}(\phi_{\Lambda'}+\phi_{\delta\Lambda};g(\Lambda))}$ . <sup>10</sup> The effect of integrating over the field modes  $\phi_{\delta\Lambda}$  is to alter the values of coefficients of the Lagrangian, yielding a new bare Lagrangian  $\mathcal{L}(\phi_{\Lambda'};g(\Lambda'))$ , which is a function of the fields with lowered cutoff  $\Lambda'$  with altered bare coefficients  $g(\Lambda')$ . Iterating this procedure by successively integrating over infinitesimal momentum shells, one obtains the continuous functional dependence  $g(\Lambda)$  of the infinite set of bare parameters on the adjustable cutoff parameter  $\Lambda$ , where  $g(\Lambda) = (g_1(\Lambda), g_2(\Lambda), g_3(\Lambda), \ldots)$ . This functional dependence is encoded in an infinite set of coupled first-order differential equations,

$$\Lambda \frac{dg_i(\Lambda)}{d\Lambda} = \beta_i(g(\Lambda), \Lambda) \tag{7}$$

and in initial conditions  $g(\Lambda_0) \equiv (g_1(\Lambda_0), g_2(\Lambda_0), g_3(\Lambda_0), ...)$  specifying the values of all bare parameters at some particular scale  $\Lambda_0$ . The beta functions  $\beta_i$  can in principle be calculated from the path integral exactly by solving the Wilson-Polchinski equation, which serves as the basis for one approach to the non-perturbative or "exact" renormalization group (Polchinski,

<sup>&</sup>lt;sup>9</sup>The "mod-squared" in parentheses is intended to signal that S-matrix elements possess an unphysical global phase, so are likely not themselves directly physical. However, squared S-matrix elements, which are used to compute the cross sections measured in accelerators, do not depend on this global phase.

<sup>&</sup>lt;sup>10</sup>Here we have assumed that in the expressions  $\mathcal{L}(\phi_{\Lambda'}; g(\Lambda'))$  and  $\mathcal{L}(\phi_{\Lambda}; g(\Lambda))$ ,  $\mathcal{L}(\phi_{\Lambda}; g)$  is the most general function of  $\phi$  allowed by the symmetries of the theory; thus, changes to the Lagrangian induced by the Wilsonian RG flow are determined entirely by changes in the coefficients g specified by the RG trajectory  $g(\Lambda)$ .

1984), (Rosten, 2012). <sup>11</sup> Assuming that the bare couplings are sufficiently small, one may also calculate the functions  $\beta_i$  perturbatively, Taylor expanding the exponential of the interaction term in the Lagrangian and then using Wick's Theorem (or its path integral equivalent) to perform the integration over the high-energy field modes  $\phi_{\delta\Lambda}$ , treating the low-energy modes  $\phi_{\Lambda'}$  as external fields. <sup>12</sup>

#### 3 The Higgs Fine Tuning Naturalness Problem

The original and perhaps most cited formulation of the Higgs fine tuning naturalness problem <sup>13</sup> rests on the observation that the leading contribution to the perturbative one-loop expansion of the (squared) Higgs pole mass  $m_p^2$  in terms of bare SM parameters gives,

$$m_p^2 = m_0^2 + \delta m^2$$
  
=  $m_0^2 - \frac{y_t^2}{8\pi^2} \Lambda_{SM}^2 + \dots$   
=  $\Lambda_{SM}^2 (\tilde{m}_0 - \frac{y_t^2}{8\pi^2}) + \dots$  (8)

where  $y_t$  is the top quark Yukawa coupling,  $\Lambda_{SM}$  the Standard Model's physical cutoff (that is, the scale at which it ceases to be empirically valid), <sup>14</sup>  $m_0^2$  is the bare Higgs mass, and  $\tilde{m}_0^2 \equiv \frac{\tilde{m}_0^2}{\Lambda_{SM}^2}$  is the dimensionless bare Higgs mass in units of  $\Lambda_{SM}$ . <sup>15</sup> The corrections  $\delta m^2$  also receive smaller contributions from lighter quarks, which can be neglected in the approximation where only the dominant correction to the Higgs bare mass is considered. By contrast with all other particle masses in the Standard Model, whose quantum corrections that depend logarithmically on the cutoff. Measurements at the LHC have further determined that  $m_p^2 = (125 \text{ GeV})^2$ , and that  $(1 \times 10^3 \text{ GeV})^2 \lesssim \Lambda_{SM}^2 \lesssim (10^{19} \text{ GeV})^2$ . While the lower limit  $(1 \times 10^3 \text{ GeV})^2$  has been set on the basis of LHC measurements, the upper limit, equal to the Planck scale, is set by theoretical expectations regarding the scales at which quantum gravitational effects can no longer be ignored. Together, these facts imply that the bare Higgs mass  $m_0^2$  must be "fine tuned" in order to recover the measured value of the physical, pole mass of the Higgs. The minimal degree of fine tuning required to recover the measured

<sup>&</sup>lt;sup>11</sup>There is a second popular approach to non-perturbative renormalization, which we do not discuss here, based on variation of an IR rather than a UV cutoff, and describing the scale dependence of parameters in the so-called effective average action, which is governed by the Wetterich equation (Wetterich, 1991), (Wetterich, 1993), (Berges et al., 2002), (Delamotte, 2012).

 $<sup>^{12}</sup>$  See, e.g., (Srednicki, 2007), Ch. 29., or (Peskin and Schroeder, 1996), Ch. 12 for details of this perturbative analysis.

<sup>&</sup>lt;sup>13</sup>We note that there exists a separate formulation of the Higgs fine tuning that concerns the running  $\overline{MS}$  Higgs mass rather than the bare Higgs mass. While the formulation considered here concerns the relationship between the Higgs bare mass (in a cutoff-based scheme) and the Higgs pole mass, the  $\overline{MS}$  formulation concerns the relationship between the  $\overline{MS}$  scalar mass in an EFT where fields much heavier than the scalar have been integrated out, and the  $\overline{MS}$  scalar in an EFT where these fields occur explicitly in the Lagrangian; see, e.g., (Skiba, 2010). We defer detailed consideration of this formulation to future work.

<sup>&</sup>lt;sup>14</sup>At leading non-trivial order perturbation theory, one can take  $y_t$  to be either a bare coupling or a renormalized coupling, since the corresponding expressions only differ at higher orders in perturbation theory.

<sup>&</sup>lt;sup>15</sup>See, for example, (Martin, 2010), for a formulation of the Higgs naturalness problem along these lines.

pole mass  $m_p^2 \sim \mathcal{O}(10^4)$  increases with the empirically established lower bound on  $\Lambda_{SM}^2$ . At the lower limit of the allowed range for  $\Lambda_{SM}$ ,  $\Lambda_{SM} = 1 \times 10^3$  GeV, the relation (8) gives,

$$\mathcal{O}(10^4) = \mathcal{O}(10^6) - \mathcal{O}(10^6)$$

while at the upper end of this range,  $\Lambda_{SM} = 10^{19}$  GeV, it gives

$$\mathcal{O}(10^4) = \mathcal{O}(10^{38}) - \mathcal{O}(10^{38}).$$

That is, the "best-case" scenario, where  $\Lambda_{SM} = 1 \times 10^3$  GeV, <sup>16</sup> requires that  $m_0^2$  and  $\delta m^2$  cancel to one part in  $10^2$  to  $10^3$ . The "worst-case" scenario, where  $\Lambda_{SM} = 10^{19}$  GeV, requires that  $m_0^2$  and  $\delta m^2$  cancel to one part in  $10^{34}$ . For many physicists, cancellation to one part in  $10^2 - 10^3$  already begins to be problematic.

There exist two conflicting attitudes toward the delicate cancellation between  $m_0^2$  and  $\delta m^2$  required to recover the measured value of  $m_p^2$  for large values of  $\Lambda_{SM}$ :

- This cancellation requires an "unlikely" "conspiracy" between the bare Higgs mass and the bare parameters that enter into the calculation of  $\delta m^2$ . The fine tuning problem can be understood as the need to explain the origin of this cancellation in terms of deeper physical theories beyond the Standard Model.
- Neither  $m_0$  nor  $\delta m^2$  is directly measurable and these quantities are therefore not physical. This opens the possibility that the delicate cancellations purported to lie at the root of the fine tuning naturalness problem are mere artifacts of mathematical representation, suggesting that the appearance of a coincidence in urgent need of explanation may therefore be illusory.

We review arguments in favor of the first view in more detail in Section 4, which served to establish naturalness as guide to model building in particle physics. The second view has had substantially fewer proponents in the literature on naturalness, but has been advanced in the work of Wetterich and Bianchi/Rovelli (Bianchi and Rovelli, 2010), (Wetterich, 1984), (Wetterich, 2012). Within the philosophical literature, Williams has more recently adopted this deflationary view of fine tuning formulations of the Higgs naturalness as grounds for characterizing naturalness in terms of inter-scale autonomy rather than fine tuning (Williams, 2015). Our discussion here will aim to show how the tension between these two views hinges on whether one physically interprets high-energy EFT's such as the Standard Model as coming equipped with a unique set of "fundamental parameters." We argue that this interpretation is motivated at least in part by a strongly literal interpretation of the well-known analogies between condensed matter field theory and the relativistic quantum field theories of high energy physics. Using Doreen Fraser's distinction, it depends on the extent to which one interprets this analogy as a "physical" analogy rather than as a merely "formal" one. Our discussion aims to develop the foundations of the deflationary view by showing how it is possible to understand EFT's in the Wilsonian picture without assuming the existence of fundamental parameters.

<sup>&</sup>lt;sup>16</sup>Current estimates place the physical cutoff of the Standard Model somewhere above 1 TeV, although precise quotes of this figure vary somewhat. For details, see http://cms-results.web.cern.ch/cms-results/ public-results/publications/EXO/index.html and https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/ CombinedSummaryPlots/EXOTICS/.

## 4 Motivating Naturalness: "Fundamental Parameters" and the High-Energy/Condensed-Matter Analogy

In this section, we examine the role of analogies between high energy and condensed matter physics, and of the notion of "fundamental parameters," in generating one set of intuitions that motivated introduction of the naturalness principle. We emphasize that the physical interpretation of certain Standard Model bare parameters as fundamental parameters closely resembles the physical interpretation of microscopic lattice parameters in certain models of condensed matter systems.

#### 4.1 Naturalness and Fundamental Parameters

In his seminal 1979 article on naturalness, Susskind explicitly introduces the notion of "fundamental parameters." He writes,

The need for fundamental scalar fields in the theory of weak and electromagnetic forces is a serious flaw. Aside from the subjective aesthetic argument, there exists a real difficulty connected with the quadratic mass divergences which always accompany scalar fields. These divergences violate a concept of naturalness which requires the observable properties of a theory to be stable against minute variations of the fundamental parameters ... [emphasis ours]

The basic underlying framework of discussion of naturalness assumes the existence of a fundamental length scale  $\kappa^{-1}$ , which serves as a real cutoff. Many authors have speculated that  $\kappa$  should be of order  $10^{19}$  GeV corresponding to the Planck gravitational length. The basic parameters of such a theory are some set of dimensionless bare couplings  $g_0$  and masses ...  $\mu_0 = \frac{m_0}{\kappa}$ . The principle of naturalness requires the physical properties of the output at low energy to be stable against very small variations of  $g_0$  and  $\mu_0$ . [emphasis ours] (Susskind, 1979).

While Susskind does rely explicitly on analogies with condensed matter physics, the bare parameters of an effective field theory (and specifically the Standard Model) at its physical cutoff are taken as fundamental in the sense that they constitute the unique, preferred parametrization of the EFT from which the EFT's predictions follow.

Schwartz's recent popular textbook on quantum field theory, which draws on the formulation of Susskind, is more explicit about the connection between naturalness and analogies to condensed matter physics. He states that "much of our intuition for fine-tuning and naturalness comes from condensed matter physics." Adopting a Wilsonian (i.e., finite-cutoff) interpretation the Standard Model, he writes,

Suppose the theory were *finite*, for example if it were UV completed into string theory, or more simply if it were the effective description of some condensed matter system (in which case  $\Lambda$  might represent some parameter of the microscopic description, such as the inverse atomic spacing). Then the bare mass m and cutoff  $\Lambda$  would be physical. In this situation, we could take the  $\Lambda^2$  divergence ... literally. ... If the scalar were the Higgs whose pole mass is  $m_p \approx 125$  GeV, and  $\Lambda$  were of the order of the Planck scale,  $\Lambda \sim M_{pl} \sim 10^{19}$  GeV, we would need  $m^2 = (1 + 10^{-34})\Lambda^2$ . This is called **fine-tuning**. Fine-tuning is a sensitivity

of physical observables (the pole mass) to variation of parameters in the theory (Schwartz, 2014), Ch. 22.

On Schwartz's presentation, bare parameters at the Standard Model's physical cutoff are physical in a sense analogous to the sense in which the parameters of certain lattice models of condensed matter systems, which characterize the interactions between adjacent atoms or molecules in the lattice, are physical. Moreover, these bare parameters are taken to be fundamental in the sense that the theory's predictions follow from them, just as macroscopic behavior of a condensed matter system follows from its microscopic dynamics. The understanding of fine tuning as sensitivity of physical observables to the variation of parameters such as the bare mass is closely tied to the understanding of fine tuning described above as relying on an "unlikely" choice of bare parameters. <sup>17</sup> This can be seen by expressing the Higgs pole mass  $m_p^2$  in terms of the dimensionless bare Higgs mass and top quark Yukawa coupling  $y_t$  (which is already dimensionless):  $m_p^2 \approx \Lambda_{SM}^2 (\tilde{m}_0^2 - \frac{y_t^2}{8\pi^2})$ . Taking  $\Lambda_{SM} = 10^{19}$  GeV and  $m_p = 10^2$  GeV, we see that a small change in either  $\tilde{m}_0^2$  or  $y_t^2$  of order, say,  $10^{-9}$  leads the value of the physical, pole mass  $m_p^2$  to jump by a factor of  $10^{27}$ . The notion that an "unlikely" delicate cancellation between  $\tilde{m}_0^2$  and  $\frac{y_t^2}{8\pi^2}$  is needed to recover the measured value of  $m_p^2$  rests on the fact that  $\frac{m_p^2}{\Lambda_{SM}^2}$  is many orders of magnitude smaller than either  $\tilde{m}_0^2$ or  $\frac{y_t^2}{8\pi^2}$ ; this, in turn, entails that slight changes in either of these dimensionless bare parameters will increase  $m_p^2$  by many orders of magnitude. In short: the presence of delicate (and therefore "unlikely") cancellations in recovering the pole mass implies delicate sensitivity of the pole mass to slight changes in the values of dimensionless bare parameters.

't Hooft adopts a similar concept of fine tuning, and emphasizes the "unlikeliness" of the cancellation necessary to recover observable values in the presence of a fundamental scalar field, which brings with it the notorious quadratic divergences. He likens the relationship between high- and low-energy parameters in a quantum field theory to the relationship between macroscopic and microscopic descriptions of a liquid or solid:

The concept of causality requires that macroscopic phenomena follow from microscopic equations. Thus the properties of liquids and solids follow from the microscopic properties of molecules and atoms. One may either consider these microscopic properties to have been chosen at random by Nature, or attempt to deduce these from even more fundamental equations at still smaller length and time scales. In either case, it is unlikely that the microscopic equations contain various free parameters that are carefully adjusted by Nature to give cancelling effects such that the macroscopic systems have some special properties [emphasis ours]. This is a philosophy which we would like to apply to unified gauge theories: the effective interactions at a large length scale, corresponding to a low energy scale  $\mu_1$ , should follow from the properties at a much smaller length scale, or higher energy scale  $\mu_2$  match with an accuracy of the order of  $\frac{\mu_1}{\mu_2}$ . That would be unnatural. ('t Hooft, 1980)

The naturalness requirement as 't Hooft formulates it is motivated by the intuition that the fundamental, microscopic, high-energy parameters do not "conspire" to give particular

<sup>&</sup>lt;sup>17</sup>Fine tuning is also associated with sensitivity of observables to fundamental parameters in the work of Barbieri and Giudice, in which they propose quantitative measures of fine tuning that quantify the rate of change of observables with respect to these parameters (Barbieri and Giudice, 1988).

macroscopic, low-energy results. Here, it is the high-energy parameters of a given EFT that are fundamental, in the sense that the values of low-energy parameters follow from them, but not the reverse.

A final important feature of the understanding of effective field theories in terms of fundamental parameters is that an effective field theory is defined fundamentally with a cutoff that is equal to its physical cutoff - that is, the UV limit of the energy scales over which the EFT is empirically valid and mathematically defined. Emphasizing this point, Peskin and Schroeder write <sup>18</sup>:

Wilson's analysis takes ... the ... point of view ... that any quantum field theory is defined fundamentally with a cutoff that has some physical significance. In statistical mechanical applications, this momentum scale is the inverse atomic spacing. In QED and other quantum field theories appropriate to elementary particle physics, the cutoff would have to be associated with some fundamental graininess of spacetime, perhaps a result of quantum fluctuations in gravity (Peskin and Schroeder, 1996) Ch. 12, p. 402.

On the interpretation of Wilsonian EFT's suggested by Schwartz, it is specifically the fundamental bare parameters defined with respect to this physical cutoff scale that uniquely serve to define the EFT, much as the direct inter-atomic interactions in some condensed matter system are sometimes modeled on a lattice with spacing equal to the physical inter-atomic distance, which comprises the physical cutoff of the material's field theoretic description.

#### 4.2 Interpreting Wilsonian EFT's in Terms of Fundamental Parameters

Here, we collect and briefly elaborate on several core features of the interpretation of Wilsonian EFT's reflected in the above quotations, which rests on the notion of fundamental parameters and (in a sense to be clarified in Section 5) a strongly "physical" reading of the analogy between high-energy and condensed-matter field theory.

An EFT is mathematically defined with a cutoff equal to its physical cutoff. In Section 2, we saw that an EFT can be non-perturbatively defined in the Wilsonian picture with a finite cutoff  $\Lambda$  and finite values for the bare parameters g. The particular understanding of EFT's suggested by the above quotations (but especially by the quotation from Peskin and Schroeder) states that in defining an EFT mathematically, we should take  $\Lambda = \Lambda_{ph}$ , where  $\Lambda_{ph}$  is the empirical scale at which the EFT in question ceases to be empirically valid - associated, for example, with the pole mass of a heavy field not included in the EFT Lagrangian, or with some fundamental graininess of spacetime associated with the onset of quantum gravitational effects. For example, QED should by this prescription be defined with a cutoff equal to the mass of the W or Z boson, beyond which the more complete description provided by electroweak theory is needed.

An EFT is defined by a single, physical, "fundamental" bare parametrization. What does it mean for a set of bare parameters to be "physical" on this view? Given Schwartz's emphasis on analogies with condensed matter systems, one reasonable interpretation is that this

<sup>&</sup>lt;sup>18</sup>Thanks to Doreen Fraser for drawing our attention to this quotation.

notion of "physical" requires that it be possible at least in principle to directly, independently measure the values of these parameters, just as one can in principle directly measure the parameters governing inter-atomic or inter-molecular interactions in a condensed matter system, without simply "working backwards" from the measured values of correlation functions. This physical set of bare parameters  $g_{ph}$ , together with the cutoff  $\Lambda_{ph}$ , are then taken as the unique parameters used to define the EFT in the manner described in Section 2.

Wilsonian RG transformations are coarse grainings of the "fundamental" bare parametrization. An EFT defined using the physical parameters  $g_{ph}$  and  $\Lambda_{ph}$  describes degrees of freedom up to the scale  $\Lambda_{ph}$ , but not above this scale. Wilsonian RG transformations, whereby one integrates out degrees of freedom from  $\Lambda_{ph}$  down to some lower scale  $\Lambda$  of interest, are then interpreted as coarse graining transformations, which throw away information about physics above the scale  $\Lambda$ . Thus, along the Wilsonian RG trajectory parametrized by  $g(\Lambda)$ , there exists one special point  $g(\Lambda_{ph}) = g_{ph}$  reflecting the true, physical, "microscopic" values of the bare parameters.

Different points along a single Wilsonian RG trajectory parametrize distinct EFT's. The process of integrating out high-energy modes from  $\Lambda_{ph}$  to  $\Lambda$  generates a separate, less encompassing EFT, defined only up to the lowered momentum cutoff  $\Lambda$ , and parametrized by  $g(\Lambda)$ . Such an EFT makes no predictions above the scale  $\Lambda$  at which the parametrization  $g(\Lambda)$  is defined. The coarse grained parameters  $g(\Lambda)$  are related to the parameters  $g_{ph}$  of the more fundamental EFT by coarse graining associated with the Wilsonian RG flow to lower momenta. Since the parametrizations  $(g(\Lambda), \Lambda)$  associated with different  $\Lambda$  are understood to have distinct domains of empirical validity, they are associated with distinct EFT's.

More formally, the understanding of Wilsonian EFT's in terms of fundamental parameters takes the physical amplitudes and pole masses predicted by the EFT to be uniquely defined by the fundamental, physical bare parameters  $g_{ph} \equiv (g_{1,ph}, g_{2,ph}, ...)$  and physical cutoff  $\Lambda_{ph}$ :

$$\begin{aligned} \mathcal{Z}[J] &= \int^{\Lambda_{ph}} \mathcal{D}\phi \ e^{i\int d^{4}x \left[\sum_{n} g_{n,ph} \mathcal{O}_{n} + J\phi\right]} \\ G^{(n)}(x_{1}, ..., x_{n}; g_{ph}, \Lambda_{ph}) &= \frac{(-i)^{n}}{\mathcal{Z}[0]} \frac{\delta^{n}}{\delta J(x_{1}) \dots \delta J(x_{n})} \bigg|_{J=0} \mathcal{Z}[J] \\ G^{(2)}(x_{1}, x_{2}; g_{ph}, \Lambda_{ph}) &= \int^{\Lambda_{ph}} \frac{d^{4}p}{(2\pi)^{4}} e^{ip(x_{1}-x_{2})} \left[ \frac{iZ(g_{ph}, \Lambda_{ph})}{p^{2} - m_{p}^{2}(g_{ph}, \Lambda_{ph})} + \int_{\sim 4m_{p}^{2}}^{\Lambda_{ph}} d\mu \frac{\rho(\mu)}{p^{2} - \mu^{2}} \right] \\ S(p_{1}, ..., p_{n}; g_{ph}, \Lambda_{ph}) &= \tilde{G}^{(n)}(p_{1}, ..., p_{n}; g_{ph}, \Lambda_{ph}) \quad \tilde{G}^{(2), -1}(p_{1}; g_{ph}, \Lambda_{ph}) ... \tilde{G}^{(2), -1}(p_{n}; g_{ph}, \Lambda_{ph}) \end{aligned}$$
(9)

All other parametrizations  $(g, \Lambda)$ , including those related to the fundamental parametrization  $(g_{ph}, \Lambda_{ph})$  by Wilsonian RG flows, are derived and less fundamental. Note moreover that on this picture, bare parameters are not a mathematically illicit crutch to be swept under the rug, but are mathematically well-defined and in fact constitute the *defining* parametrization of the EFT. The interpretation of Wilsonian QFT's in terms of fundamental parameters has several important virtues by comparison with the pre-Wilsonian understanding of perturbative renormalization, according to which bare parameters were formally infinite and therefore unphysical.

First, it has the advantage of making the theory mathematically well-defined and avoiding the divergences that arose in older approaches to perturbative renormalization. Every quantity calculated in the theory can in principle be associated with a finite number. Thus, one avoids the conceptual and mathematical obscurity that arises in attempting to deal with the infinite quantities that arise on pre-Wilsonian approaches.

Second, beyond the question of mathematical well-defined-ness, there may be something deeply intuitively appealing about the view of bare parameters as fundamental parameters, and more generally with the strategy of interpreting quantum field theories in high energy physics by direct analogy with condensed matter systems, where one has a relatively clear physical picture of the relationship between macroscopic phenomenology and microscopic degrees of freedom. By transplanting this intuitive condensed matter picture into the context of elementary particle physics, one similarly gains a clear (although not necessarily wholly accurate) picture of the underlying physical degrees of freedom, and of the manner in which the phenomenology of elementary particle physics emerges from them at a coarse grained level.

#### 4.3 Higgs Fine Tuning and Fundamental Parameters

On the view just described, an EFT is fundamentally specified by a particular set of bare parameters  $g_{ph}$  and a particular cutoff  $\Lambda_{ph}$ , while quantities such as pole masses, scattering amplitudes, and bare parameters  $g(\Lambda)$  for  $\Lambda < \Lambda_{ph}$  are all understood as deriving from these. The cutoff and bare parameters  $g_{ph}$  are thus taken mutually *independent* inputs into the mathematical formalism of an EFT model on this view. Assume that the fundamental parameters are "chosen by nature" via sampling from a reasonably smooth probability measure over the fundamental bare parameter space. Then the relation  $m_p^2 \approx \Lambda_{SM}^2 (\tilde{m}_0^2 \frac{y_t^2}{8\pi^2}$ ) suggests that it is overwhelmingly likely, given a large value of the physical cutoff  $\Lambda_{SM}$ , that a random sampling of  $\tilde{m}_0^2$  and  $y_t$  will yield a pole mass  $m_p^2$  of order  $\Lambda_{SM}^2$ . That is, "natural" values for  $m_p^2$  are on the order of  $\Lambda_{SM}^2$ . Only for an extremely atypical and unlikely subset of the bare parameter space of values for  $\tilde{m}_0$  and  $y_t$  do there arise the delicate cancellations necessary to recover  $m_p^2 \ll \Lambda_{SM}^2$ . Recalling the micro/macro analogy of 't Hooft, the sheer unlikeliness of such a choice, as viewed from the perspective of Standard Model effective field theory (SMEFT), suggests a sort of deeper underlying "conspiracy" between the "microscopic" bare parameters  $\tilde{m}_0^2$  and  $y_t$  to yield a particular value for the "macroscopic" quantity  $m_p^2$ . Put differently, the unlikeliness of the coincidence that must occur for  $\tilde{m}_0^2$  and  $y_t$  to give small values for the pole mass demands explanation in terms of a deeper, more encompassing BSM theory. The absence of such an explanation within the Standard Model is the feature that is perhaps most often associated with the Higgs naturalness problem. <sup>19</sup>

<sup>&</sup>lt;sup>19</sup>Building on earlier arguments by Anderson and Castaño in (Anderson and Castano, 1995), Hossenfelder has recently argued in (Hossenfelder, 2018) that the need to assume a smooth probability distribution over the SM parameter space constitutes a weak link in naturalness-based reasoning: what could justify the choice of such a probability distribution, given that the universe appears to sample only one set of values from this space? While we regard this as an important source of skepticism about fine tuning arguments, we focus here on a separate source of concern as to whether there even exists a unique space of fundamental

## 5 "Formal" vs. "Physical" Views of the High-Energy/Condensed-Matter Analogy

Previously, we described the notion of fundamental parameters as resting on an especially "literal" or "physical" interpretation of the analogy between condensed matter theory and high energy physics. To clarify our meaning, and to underscore the contrast with the alternative view of Wilsonian EFT's described in the next section, it will be useful to employ a distinction between "formal" and "physical" analogies, which has recently been developed in the work of D. Fraser and of D. Fraser & A. Koberinski (Fraser, 2018), (Fraser and Koberinski, 2016).

According to Fraser, a "formal" analogy occurs when the same mathematical formalism can be applied in physically distinct contexts. For example, one can apply the wave equation to the description of sound waves and electromagnetic waves, which constitute strongly physically distinct domains of application. The formal analogy between high-energy physics and condensed matter physics is evidenced by the fact that in both contexts, one finds the application of path integrals, Feynman diagrams, the renormalization group, and spontaneous symmetry breaking (SSB), to name a few of the main points of structural commonality.

Within Fraser's view, not all formal analogies are physical analogies. She and Koberinski describe the difference by saying that "formal analogies map similar elements of the mathematical formalism of the models; physical analogies map elements of the models with similar physical interpretations" (Fraser and Koberinski, 2016). Naturally, this raises the question of what constitutes similarity of physical interpretation. For our purposes here, it will be sufficient to illustrate the core idea of the distinction by way of example, beginning with a case discussed by Fraser and Koberinski.

As an example of an analogy that is formal but not physical, Fraser and Koberinski consider the analogy between SSB in the SM Higgs mechanism and in the BCS and Ginzburg-Landau theories of superconductivity. Here, they note that while in condensed matter systems, SSB is a process that can occur through time, in the framework of the Standard Model (in ordinary rather than finite-temperature quantum field theory), the parameters are fixed for all time so that symmetry breaking may not be understood as a temporal process. <sup>20</sup> Thus, while similar mathematical formalisms are employed across the analogy, the physical interpretation of this formalism differs dramatically between the two contexts.

A second example of an analogy that might be taken as formal but not physical is the analogy between the theory of electromagnetic waves and the theory of mechanical waves (e.g., sound waves). Whereas sound waves propagate in a mechanical medium and their behavior can often be derived on the basis of classical mechanical models of this medium, electromagnetic waves do not arise as disturbances within such a mechanical medium. Nevertheless, the thought that electromagnetic waves might arise as disturbances in such a medium inspired the unsuccessful attempts in the nineteenth century to formulate an ether theory of light. Thus, efforts to formulate such an ether theory could be characterized in Fraser's terms as falsely supposing the analogy between sound waves and electromagnetic waves to be a physical rather than merely formal analogy.

In regard to the Higgs naturalness problem, the interpretation of bare SM parameters

parameters over which to define this probability distribution.

 $<sup>^{20}</sup>$ On the other hand, their claim may not extend to SSB in the more general framework of finite-temperature quantum field theory.

as fundamental parameters may reasonably be characterized as extending the established formal analogy between high energy and condensed matter physics - characterized by the common formalism of path integrals, Feynman diagrams, renormalization group, and SSB to a physical analogy. It does so by supposing the existence of a physically preferred, "fundamental" bare parametrization at the SM's physical cutoff, just as in certain condensed matter systems there exists an underlying microscopic lattice description that directly characterizes the microscopic interactions of the atoms in the lattice. The notion that there is a single, true, "microscopic," fundamental bare parametrization for any given high-energy EFT goes beyond recognition of the mathematical similarities between high energy and condensed matter theory to attribute analogous physical interpretations to the bare parameters that occur in field theories across both contexts. In (Fraser, 2018), Fraser provides a detailed, systematic investigation of the analogy between condensed matter field theory and relativistic quantum field theory in Wilson's work on the renormalization group; she argues that this analogy is merely formal, including with regard to the interpretation of parameters such as the bare mass. One of our central goals here is to clarify the implications of this view - that the high-energy/condensed-matter analogy is merely formal - for the Higgs naturalness principle, and more generally for the interpretation of bare parameters and Wilsonian renormalization group transformations in the context of high-energy physics.<sup>21</sup>

Where the physical interpretation of bare parameters between high energy and condensed matter field theory is concerned, it is important to note that bare parameters in condensed matter models are not always taken to directly represent the microscopic interactions between adjacent atoms and molecules in the material being described. In many cases, the bare parameters are artificially tuned to fit measurements of correlation functions characterizing the material's coarse grained macroscopic behavior, and are not taken to represent the microscopic dynamics of the material. Nevertheless, the particular cases from condensed matter physics that appear to inform Schwartz's physical interpretation of bare parameters in high energy physics are the cases in which the parameters of a condensed matter lattice model do directly represent the microscopic, inter-atomic interactions of the system; for examples of such cases, see e.g. (Kittel et al., 1996), Ch.'s 1-4.

## 6 Deflating Naturalness: Absence of Fundamental Parameters

We now turn to consider the second, deflationary view of Higgs fine tuning described in Section 3, which has been advocated by Wetterich, Bianchi/Rovelli, and Williams, and which regards fine tuning of bare parameters as unproblematic.

Wetterich writes in (Wetterich, 1984) that "fine tuning of bare parameters is not really the relevant problem: we do not need to know the exact formal relation between physical and bare parameters (which furthermore depends on the regularization scheme), and it is not important if some particular expansion method needs fine tuning in the bare parameters or not." Bianchi and Rovelli express a similar point of view in the context of the cosmological constant problem, which is structurally similar to the Higgs naturalness problem, but

 $<sup>^{21}</sup>$ Nevertheless, we wish to highlight as a potential caveat that the formal/physical distinction may not be sharply defined. All pairs of physical systems must be physically disanalogous in *some* sense - otherwise, they would be the same system. Thus, as a qualification to Fraser's distinction, we adopt the view that no analogy is physical *simpliciter*, but rather only physical *with respect to* particular aspects of the analogy, such as (in our case), the status of bare parameters.

more severe in that it arises from a delicate cancellation between quartically (rather than quadratically) divergent quantities. They write, "simple physical arguments indicate that the vacuum energy itself cannot be 'real' in the sense of gravitating: if it did, any empty box containing a quantum field would have a huge mass, and we could not move it with a force, since gravitational mass is also inertial mass. On physical grounds, vacuum energy does not gravitate ... A shift in the vacuum energy does gravitate." (Bianchi and Rovelli, 2010). Bianchi and Rovelli deny that we should ascribe direct physical significance to the value of a bare parameter - in this case, the bare vacuum energy. For this reason, they claim that contrary to the dictates of naturalness, "there is no great mystery" in the smallness of the cosmological constant. More recently, Williams has argued against the formulation of naturalness as a prohibition against fine tuning of bare parameters as follows: "stuck with an effective theory, one is free to arrange the values of free parameters at high energy - those appearing in the original Lagrangian at the original cutoff scale - however is needed to make accurate predictions for empirically accessible low energy physics, which is all the EFT can reasonably purport to describe anyway. The only concern in doing this is that one isn't fooled into thinking that by being forced to make specific choices for the values of the high-energy parameters, they have thereby learned something meaningful about physics near the cutoff scale" (Williams, 2015).  $^{22}$ 

In characterizing fine tuning of bare parameters as unproblematic, these authors seem implicitly to regard arguments based on the notion of fundamental bare parameters as unconvincing. In this section, we seek to clarify one possible set of foundations for this view - in particular, we describe one way of formulating and interpreting Wilsonian effective field theories that goes entirely without the notion of fundamental parameters.

#### 6.1 Wilsonian EFT's without Fundamental Parameters

We have seen that quantities such as S-matrix elements and pole masses are left exactly invariant under re-parametrization by Wilsonian RG transformations. Thus, many choices of the parameters  $(g(\Lambda), \Lambda)$  yield the same values for these quantities. This suggests that the notion of a unique, physically preferred, "fundamental" bare parametrization constitutes an idle, dispensable posit in the definition of a Wilsonian EFT - both from the perspective of generating the EFT's successful empirical predictions and from the perspective of ensuring that the EFT is finite and mathematically well defined. This hypothesis suggests one way of formulating Wilsonian EFT's without fundamental parameters. We now review the main features of this formulation.

*Physical quantities as Wilsonian RG invariants:* The only quantities calculated within a given EFT that may represent physical quantities - as opposed to quantities that depend on an arbitrary mathematical convention, such as choice of gauge or renormalization scheme

 $<sup>^{22}</sup>$ As Williams observes, Wetterich does not deny that naturalness problems exist, but only that, in order to be seen as genuine problems, they should be formulated in terms of "physical," renormalized parameters. However, we think it worth noting on this point that renormalized parameters need not always be physical parameters. For example, while the pole mass and renormalized  $\overline{MS}$  mass are both renormalized parameters (albeit in different schemes), it is reasonable to question whether the running  $\overline{MS}$  mass is genuinely physical in the same sense that pole mass is: while calculations of the pole mass must yield the same results irrespective of renormalization scheme, and across different effective field theories, the  $\overline{MS}$  mass is specific to a particular scheme and its value is not generally preserved across matching between different EFT's.

- are invariant under re-parametrization by Wilsonian RG transformations. For example, the pole mass and S-matrix elements are admitted as candidates for physicality since they possess this invariance:

$$\Lambda \frac{d}{d\Lambda} S(p_1, ..., p_N; g(\Lambda), \Lambda) = 0$$
  
$$\Lambda \frac{d}{d\Lambda} m_p^2(g(\Lambda), \Lambda) = 0$$

The invariance of these quantities follows from the Wilsonian RG invariance of the n-point Green's functions:

$$\Lambda \frac{d}{d\Lambda} \tilde{G}(p_1, ..., p_N; g(\Lambda), \Lambda) = 0$$
(10)

which in turn follows from the invariance of the partition function:  $\Lambda \frac{d}{d\Lambda} Z[J; g(\Lambda), \Lambda] = 0$ . <sup>23</sup> However, we should note that since S-matrix elements contain an arbitrary global phase, it is rather mod-square S-matrix elements that one might choose to regard as physical. Thus, in the view of Wilsonian EFT's sketched here, Wilsonian RG invariance constitutes a necessary but not sufficient condition for physicality. By contrast, on the "fundamental parameters" interpretation of Wilsonian EFT models, a single set of values for the cutoff and bare parameters, which are manifestly not invariant under Wilsonian RG flow, are also regarded as physical - i.e., in principle, one could measure them directly and independently, rather than "working backwards" to their values from measured values of pole masses and cross sections.

Wilsonian RG transformations as invertible re-parametrizations: In the absence of fundamental parameters, Wilsonian RG transformations are regarded as re-parametrizations that transform between physically equivalent, finite representations of the same physics, rather than as coarse grainings of a single "microscopic," high-energy description, associated with the physical-cutoff bare parametrization  $g(\Lambda_{ph}) = g_{ph}$ . A change of scale  $\Lambda$  and parameters  $g(\Lambda)$  associated with the Wilsonian RG flow does not signal passage to a more or less fundamental EFT, but merely passage to a different finite parametrization of the same EFT. Thus, within a single EFT, one may represent S-matrix elements and pole masses using a low value  $\Lambda_l$  of the unphysical reference scale  $\Lambda$ , or a high value  $\Lambda_h$ :

$$S(p_1, ..., p_n; g(\Lambda_l), \Lambda_l) = S(p_1, ..., p_n; g(\Lambda_h), \Lambda_h) \equiv S(p_1, ..., p_n)$$
$$m_p^2(g(\Lambda_l), \Lambda_l) = m_p^2(g(\Lambda_h), \Lambda_h) \equiv m_p^2.$$

Thus, it is not the case that bare parameterizations  $g(\Lambda_h)$  referenced to a high cutoff parameter scale  $\Lambda_h$  are more fundamental than bare parametrizations  $g(\Lambda_l)$  referenced to a low cutoff parameter scale  $\Lambda_l$ , if greater fundamentality is understood to require that the more fundamental description strictly contain the range of phenomena described by the less fundamental description, and describe these phenomena in greater accuracy and/or detail. Contrary to the suppositions of the "fundamental parameters" view, the low-scale

 $<sup>^{23}</sup>$ Note that the Callan-Symanzik equation follows directly from (10) via application of the Chain Rule.

parametrization  $(g(\Lambda_l), \Lambda_l)$  captures precisely the same set of physical phenomena as the high-scale parametrization  $(g(\Lambda_h), \Lambda_h)$ , and is no less physically encompassing. This feature is explained further in subsections 6.2 and 6.3.

An EFT is associated with an entire Wilsonian RG trajectory, not just a single point on such a trajectory: On the understanding of Wilsonian RG transformations as mere changes of parametrization within a single EFT, it is more appropriate to associate a given EFT not with any single parametrization, but with the entire continuum of physically equivalent, finite parametrizations that lie along the EFT's Wilsonian RG trajectory. Thus, the EFT is not uniquely associated with any single point along a Wilsonian RG trajectory, but with the entire trajectory itself, which represents the one-parameter equivalence class of mathematically well-defined parametrizations, all of which yield exactly the same set of physical amplitudes. While any single point along a Wilsonian RG trajectory serves to define the whole trajectory via the Wilsonian RG equations, it is unnecessary for the purpose of generating the EFT's successful empirical predictions to single out any particular such point as providing the unique physically correct "microscopic" parametrization of the theory. Thus, the approach to EFT's without fundamental parameters retains the advantage that the EFT as defined in this manner is finite (since it is defined by an equivalence class of finite parametrizations), but relinquishes the assumption that any single finite parametrization is physically preferred or fundamental.

What then is the physical significance of the Wilsonian RG flow, given that it merely represents a mere change of parametrization? In part, the answer lies in the implications of this flow for the variation of S-matrix elements as the physical, external momenta  $p_i$  are scaled uniformly by some real number s:

$$S(sp_1, ..., sp_N; g(\Lambda), \Lambda) = \left[s^{2-d} \frac{Z(\Lambda)}{Z(s\Lambda)}\right]^{-N/2} S(p_1, ..., p_N; g(s\Lambda), s\Lambda),$$
(11)

where  $Z(\Lambda) \equiv g_1(\Lambda)$ . Thus, given the Wilsonian RG trajectory  $g(\Lambda)$ , the predictions of the theory for  $S(p_1, ..., p_N)$  are defined up to scales for which the RG trajectory is mathematically defined. Note that, in cases where the Wilsonian RG trajectories of two theories agree approximately at small  $\Lambda$ , but diverge for large  $\Lambda$ , the predictions for  $S(p_1, ..., p_N)$  should be approximately equal for small values of the physical scales  $p_i$  but differ substantially for large  $p_i$ .

The physical cutoff of an EFT does not occur in the mathematical definition of that EFT: It is important to note that in defining an EFT by a one-parameter equivalence class of finite parametrizations  $(g(\Lambda), \Lambda)$ , the physical cutoff  $\Lambda_{ph}$  of an EFT appears nowhere in the mathematical definition of that EFT. Without assuming the existence of a preferred set of fundamental parameters, one still obtains the same predictions for physical quantities for any parametrization  $(g(\Lambda), \Lambda)$  for which the RG trajectory is defined. Certainly, one is free as a matter of arbitrary convention to set  $\Lambda = \Lambda_{phys}$ , but nothing is gained in terms of scope or accuracy of the EFT by doing so. The scale  $\Lambda_{ph}$  is purely a reflection of the fit between the EFT model and the world;  $\Lambda_{phys}$  must be determined empirically. While it is an offrepeated claim that EFT's predict their own breakdown in the UV, this is true only in the attenuated sense that the Wilsonian RG trajectory may cease to be mathematically defined at some upper limit  $\Lambda^*$  for  $\Lambda$ , as in cases where the theory possess a Landau pole. Beyond the relatively weak requirement that  $\Lambda_{ph} < \Lambda_*$ , nothing about the intrinsic mathematical definition of the EFT tells us the precise value of  $\Lambda_{ph}$ . While one is free to define an EFT with cutoff  $\Lambda_{ph}$ , in doing so one must insert this value of the cutoff by hand. Moreover, it is relevant to note that the scale  $\Lambda_{ph}$  at which the EFT ceases to be empirically valid is not even defined until one fixes the parameters  $g(\Lambda)$  at some  $\Lambda$  (thus fixing the predictions of the EFT) and until one sets the margin of error within which the EFT's predictions are considered empirically valid. On this view, the physical cutoff  $\Lambda_{phys}$  of an EFT is no more intrinsic to the mathematical definition of that EFT than the speed of light c is intrinsic to the mathematical definition of models in Newtonian mechanics.

Perhaps the strongest motivation for adopting this view of EFT's is that it sheds an idle assumption of the view based on fundamental parameters - namely, the very existence of a physically preferred bare parametrization. As we have seen, the assumption that there exists a single physically preferred set of values for the bare parameters is neither necessary for generating the theory's empirical predictions, nor for defining the theory in a way that is finite and mathematically consistent. The act of nevertheless positing such a unique set of fundamental parameters thus carries a strongly *ad hoc* character. <sup>24</sup> By contrast, in the physical setting of condensed matter systems, the assumption that there exists a single, physically fundamental microscopic parametrization, *is* supported by independent evidence and is *not ad hoc*, since these parameters can be measured directly (i.e., without simply tuning them to measured values correlation functions).

A second argument for shedding the notion of fundamental parameters is that even in cases where it is possible in practice to experimentally probe physics at or above the scale of an EFT's physical cutoff, we do not directly measure the bare parameters at this cutoff. For example, although it is possible to probe physics near the physical cutoff of QED - around the pole mass of the W boson - one does not directly measure the bare parameters of QED; one only ever tunes these parameters to possess whatever values are necessary to recover the measured values of cross sections and pole masses. This an important point of physical dis-analogy with the case of condensed matter systems, where it is possible to directly probe the microscopic interactions between adjacent lattice sites that ultimately underwrite the success of condensed matter models in describing the system's collective behavior.<sup>25</sup>

A third point in favor of shedding the notion of fundamental parameters applies in certain conceivable scenarios for physics beyond the Standard Model, in which the Higgs pole mass enters as a basic input to the fundamental theory - let us call it  $T_{new}$ . In such cases, it cannot be true that the bare parameters  $g(\Lambda_{phys})$  of the Standard Model at its physical cutoff are physically more fundamental than the Higgs pole mass. It makes little sense to countenance  $m_p^2$  as fundamental in  $T_{new}$  but as non-fundamental in SMEFT, given that SMEFT is only a low-energy approximation to  $T_{new}$ . In this case, it is clear that the bare Higgs mass  $m^2(\Lambda_{SM})$  is not fundamental or directly physical, but is artificially tuned to whatever value

 $<sup>^{24}</sup>$  For recent philosophical analysis of *ad hoc*'ness in science with a focus on cases in elementary particle physics, see Friederich, Harlander, and Karaca's (Friederich et al., 2014)  $^{25}$ We emphasize, however, that in many cases bare parameters occurring the field theoretic description

<sup>&</sup>lt;sup>25</sup>We emphasize, however, that in many cases bare parameters occurring the field theoretic description of condensed matter systems are NOT understood to directly represent the microscopic interactions in the material. Rather, one simply "works backward" from the measured values of correlation functions and macroscopic quantities to the values of bare parameters in one's chosen renormalization scheme; in such schemes, the bare parameters do not have the physical interpretation as representing microscopic interactions in the material. Even in such cases, one nevertheless understands the success of the condensed matter model as rooted in an underlying microscopic lattice description (at least, in the case of solids), from which the values of macroscopic variables describing the material's collective behavior are derived. The parameters governing such microscopic interactions *are* fundamental parameters. Thanks to an anonymous referee for emphasizing this point.

it must possess to recover the measured values of genuinely physical quantities such as the Higgs pole mass.

A final weaker argument, which is nevertheless worth noting briefly, is that since the "fundamental parameters" view takes the state space and dynamics of an EFT to be truncated in the UV by  $\Lambda_{phys}$ , the EFT makes no predictions about phenomena above the scale of  $\Lambda_{phys}$ . The state space simply does not possess the states to describe scattering processes at physical scales (e.g. center-of-mass energy, momentum transfer) above  $\Lambda_{phys}$ . For this reason, the "fundamental parameters" view seems inconsistent with the conventional notion that QED is also capable of making predictions (albeit not empirically correct ones) about phenomena above the scale of its physical cutoff. By contrast, the view of EFT's as defined by an entire Wilsonian RG trajectory  $g(\Lambda)$ , rather than the single point  $g(\Lambda_{phys})$ , accommodates this fact naturally, since the EFT's Hilbert space (which can be constructed from the correlation functions) is defined up to all scales for which the RG trajectory is defined, and not just up to the physical cutoff scale.

We now consider two closely related objections to the view of Wilsonian EFT's without fundamental parameters that we have just sketched.

#### 6.2 Objection 1: Aren't Wilsonian RG Transformations Coarse Graining Transformations?

The Wilsonian RG flow from high to low scales is often regarded as a coarse graining transformation. However, this point requires some care, since the Wilsonian RG equations,

$$\Lambda \frac{d}{d\Lambda} g_i(\Lambda) = \beta_i(g(\Lambda), \Lambda) \tag{12}$$

are first-order in  $\Lambda$  and therefore invertible. As Morris has emphasized, there is no "loss of information" in the Wilsonian RG flow from a parametrization  $g(\Lambda_h)$  defined at some high scale  $\Lambda_h$  to the corresponding parametrization  $g(\Lambda_l)$  at a low scale  $\Lambda_l$  (Morris, 1994), (Morris, 1998). One can run the parameters  $g(\Lambda)$  up as well as down in  $\Lambda$ .

What then of the notion that the Wilsonian RG explains why theories differing in their description of physics at high-energies all converge to the same renormalizable theory at low energies? Surely information about the details of physics at high energies is lost in transition to describing low-energy phenomena by a renormalizable theory, so that the Wilsonian RG flow can be regarded as coarse graining. Reconciliation can be found in the fact that information is lost only in the approximation where small coefficients of irrelevant operators are ignored, which entails a change to a distinct RG trajectory. Thus, it is not the Wilsonian RG flow in itself that constitutes coarse graining, but this flow combined with the added step of throwing away information about these small coefficients. Prior to performing this second step, the Wilsonian RG flow can be regarded as an invertible re-parametrization of a fixed set of physical amplitudes.

It is worth noting here that while the process of integrating out infinitesimal momentum shells for a single fixed field or set of fields is invertible in the absence of approximations, the process of integrating out an entire field from the path integral in order to obtain the path integral for an EFT describing some smaller set of fields is *not* generally invertible and so *can* be regarded as a coarse graining. Starting from a theory of two fields, one light field  $\phi$  and one heavy field  $\psi$  - where "light" and "heavy" are understood in terms of the pole masses of the fields - one can define an EFT describing the behavior of only the light field at low energies (where particles of the heavy field are not created), by "integrating out" the heavy field  $\psi$  from the path integral of the full theory. The full theory describing both fields  $\phi$  and  $\psi$  - which may itself be a low-energy approximation to some still more encompassing theory - is more fundamental than the EFT describing only the light field  $\phi$  in the sense that the full theory circumscribes the domain of empirical validity of the light field EFT; the light field EFT thus "reduces to" the full theory. <sup>26</sup> Consequently, the parameters  $g_{\phi}(\Lambda), g_{\phi\psi}(\Lambda), g_{\psi}(\Lambda)$  of the full theory (where  $g_{\phi\psi}(\Lambda)$  correspond to operators that couple  $\phi$  and  $\psi$ ) do constitute a more fundamental parametrization of light-field amplitudes than do the parameters  $g'_{\phi}(\Lambda)$  of the light field EFT. <sup>27</sup> Thus, the progression from a more to a less fundamental parametrization occurs not in the flow to smaller values of  $\Lambda$ , but in the projection of the RG flow of the full theory onto the RG flow of the light field EFT, which in principle can be performed at arbitrary  $\Lambda$ .

# 6.3 Objection 2: Doesn't Larger $\Lambda$ Imply a More Encompassing Theory?

One assumption of the interpretation of Wilsonian EFT's based on fundamental parameters is that a theory parametrized at scale  $\Lambda$  only describes phenomena at physical scales below  $\Lambda$ . Thus, parametrizations  $g(\Lambda_h)$  with respect to a high cutoff  $\Lambda_h$  describe a distinct, more fundamental theory than do parametrizations  $g(\Lambda_l)$  with respect to a lower cutoff  $\Lambda_l$ . While nothing prevents one from defining EFT's in this manner, such an interpretation is not necessitated by the mathematical formalism of the Wilsonian RG. Other interpretations of this formalism are also possible. In particular, in the interpretation sketched in subsection 6.1, any point  $g(\Lambda)$  along the Wilsonian RG trajectory can be used to parametrize the full set of physical amplitudes predicted by that EFT. The unphysical scale parameter  $\Lambda$  is independent of the physical scales of the problem (e.g., pole masses, external momenta  $p_i$ ), and there is no special need for  $\Lambda$  to lie above (or below) these physical scales.

One can see this by noting that

$$\Lambda \frac{d}{d\Lambda} Z[J;g(\Lambda),\Lambda] = 0,$$

where  $g(\Lambda)$  is a solution to the Wilsonian RG equations (12), so that we can write  $Z[J; g(\Lambda), \Lambda] = Z[J]$ . That is,  $Z[J; g(\Lambda), \Lambda]$  is the same function of J irrespective of the value chosen for  $\Lambda$ . In particular, the functional derivatives of Z[J] with respect to J do not depend on  $\Lambda$ .

$$\tilde{G}^{(n)}(p_1,...,p_n) = \frac{(-i)^n}{\mathcal{Z}[0]} \frac{\delta^n}{\delta \tilde{J}(p_1) \dots \delta \tilde{J}(p_n)} \bigg|_{J=0} \mathcal{Z}[J].$$

From this it follows that

<sup>&</sup>lt;sup>26</sup>Within the philosophical literature, the subjects of reduction and emergence as they relate to renormalization and effective field theory have been examined at length in the work of Butterfield, Hartmann, Castellani, Bain, Crowther, Huggett, Williams, Franklin, and others (Butterfield, 2014), (Hartmann, 2001), (Castellani, 2002), (Bain, 2013), (Crowther, 2015), (Huggett and Weingard, 1995), (Williams, 2017), (Franklin, 2017). Recent discussion concerning the general methodology of reduction in physics can be found in Butterfield, Crowther, Fletcher, and Rosaler (Butterfield, 2011a), (Butterfield, 2011b), (Butterfield and Bouatta, 2012), (Butterfield, 2014), (Fletcher, 2015), (Crowther, 2015), (Crowther, 2017), (Rosaler, 2015), (Rosaler, 2017), (Rosaler, 2013).

<sup>&</sup>lt;sup>27</sup>Note that the parameters  $g'_{\phi}(\Lambda)$  of the light field EFT differ from the light field parameters  $g_{\phi}(\Lambda)$  of the full theory since they are subject to so-called "matching corrections" that reflect the influence of heavy fields that have been integrated out.

$$\begin{split} \Lambda \frac{a}{d\Lambda} G(p_1,...,p_N;g(\Lambda),\Lambda) &= 0 \\ & \downarrow \\ G(p_1,...,p_N;g(\Lambda),\Lambda) &= G(p_1,...,p_N) \\ S(p_1,...,p_N;g(\Lambda),\Lambda) &= S(p_1,...,p_N) \\ & m_p^2(g(\Lambda),\Lambda) = m_p^2. \end{split}$$

As Wilsonian RG invariants, the quantities  $G(p_1, ..., p_N)$ ,  $S(p_1, ..., p_N)$ , and  $m_p^2$  belong to the set of quantities that may potentially be regarded on this interpretation as "physical." These equations illustrate a sense of cutoff independence that does not require the existence of a continuum limit, where  $\Lambda$  is taken to infinity - rather, the explicit cutoff dependence of quantities such as S-matrix elements and pole masses is removed at *finite*  $\Lambda$  by the cutoff dependence of the parameters  $g(\Lambda)$ .

The parameter  $\Lambda$  can be interpreted as an unphysical reference scale, which sets the boundary between those modes  $\tilde{\phi}(k)$  in the path integral that have been explicitly integrated over, with their influence absorbed into the Lagrangian parameters  $g(\Lambda)$ , and those that have not been explicitly integrated over, so that they appear explicitly in the Lagrangian of the path integral. One can understand  $\Lambda$ 's role in partial analogy to the simple case of bivariate integration:

$$F[j] \equiv \int dx \, dy \, f(x, y; j) = \int dx \, g(x; j) \tag{13}$$

where  $g(x; j) \equiv \int dy \ f(x, y; j)$ . The function F[j] and its derivatives with respect to jare unchanged by whether we write F[j] as the integral over  $dx \ dy$  of f(x, y; j) or as the integral over dx of g(x; j). Likewise, the functional Z[J] and its derivatives with respect to J are unchanged by whether we write Z[J] as a functional integral over modes below  $\Lambda_1$  of  $e^{iS(g(\Lambda_1))}$  or as a functional integral over modes below  $\Lambda_2$  of  $e^{iS(g(\Lambda_2))}$  (where  $\Lambda_1 \neq \Lambda_2$ ). The parameter  $\Lambda$ , which simply reflects how we choose to write down the expression for the path integral, is thus unrelated to the physical scale set by the external momenta  $p_i$ , and may lie above or below them. For this reason, parametrizations associated with larger  $\Lambda$  need not be identified with distinct, more encompassing theories. It is reasonable to regard them instead as alternative parametrizations of a single EFT, since all such parametrizations represent one and the same set of physical amplitudes, derived from the same cutoff-independent function Z[J]. On this interpretation, the parameter  $\Lambda$  should therefore not be understood as a cutoff in the particular sense that it truncates the Hilbert space or the set of field modes over which the dynamics of the theory are defined.

From the above considerations, it follows that we can use any parameters  $g(\Lambda)$  along the Wilsonian RG flow - not just  $g(\Lambda_{phys})$ , and not just  $g(\Lambda)$  for  $\Lambda > p_i, m_p, etc.$  - to parametrize correlation functions and physical quantities derived from them. More formally, the equations that define an EFT's correlation functions and S-matrix elements in the absence of fundamental parameters take the form,

$$\begin{aligned} \mathcal{Z}[J] &= \int^{\Lambda} \mathcal{D}\phi \ e^{i\int d^{4}x \left[\sum_{n} g_{n}(\Lambda)\mathcal{O}_{n} \ + \ J\phi\right]} \\ G^{(n)}(x_{1},...,x_{n};g(\Lambda),\Lambda) &= \frac{(-i)^{n}}{\mathcal{Z}[0]} \frac{\delta^{n}}{\delta J(x_{1}) \ ... \ \delta J(x_{n})} \bigg|_{J=0} \mathcal{Z}[J] \\ G^{(2)}(x_{1},x_{2};g(\Lambda),\Lambda) &= \int^{\Lambda} \frac{d^{4}p}{(2\pi)^{4}} e^{ip(x_{1}-x_{2})} \left[ \frac{iZ(g(\Lambda),\Lambda)}{p^{2} - m_{p}^{2}(g(\Lambda),\Lambda)} + \int_{\sim 4m_{p}^{2}}^{\Lambda} d\mu \frac{\rho(\mu)}{p^{2} - \mu^{2}} \right] \\ S(p_{1},...,p_{n};g(\Lambda),\Lambda) &= \tilde{G}^{(n)}(p_{1},...,p_{n};g(\Lambda),\Lambda) \ \tilde{G}^{(2),-1}(p_{1};g(\Lambda),\Lambda)...\tilde{G}^{(2),-1}(p_{n};g(\Lambda),\Lambda), \end{aligned}$$
(14)

where any  $\Lambda$  for which the Wilsonian RG flow is defined may be used to parametrize the theory. As Morris has noted, one can even take  $\Lambda \to 0$  without changing the values of the correlation functions, or any of the quantities derived from them. By contrast with the formulation given in (9), no single parametrization is "fundamental."

#### 6.4 Higgs Fine Tuning without Fundamental Parameters

On shedding the assumption that a single set of values of the parameters g constitute a physically preferred set of fundamental parameters, the bare parameters at a given scale are no longer mutually independent. Instead, they are constrained to lie within a one-parameter class of physically equivalent finite parametrizations, each associated with a different value of the unphysical scale parameter  $\Lambda$ , all of which give the same values for the Higgs pole mass and correlation functions. Noting that the bare Higgs mass  $m_0^2(\Lambda)$  and Yukawa coupling  $y_t(\Lambda)$  can be interpreted as two of the parameters  $g(\Lambda)$  in the cutoff path integral Lagrangian for the Standard Model, the leading contribution to the one-loop expansion of the pole mass at  $\Lambda$  gives:

$$m_p^2 = m_0^2(\Lambda) + \delta m^2(\Lambda)$$
  
=  $m_0^2(\Lambda) - \frac{y_t^2(\Lambda)}{8\pi^2}\Lambda^2 + \dots$   
=  $\Lambda^2 \left( \tilde{m}_0^2(\Lambda) - \frac{y_t^2(\Lambda)}{8\pi^2} \right) + \dots$  (15)

where  $\tilde{m}_0^2 = \frac{m_0^2}{\Lambda^2}$ . The scale parameter  $\Lambda$  is chosen as a matter of convention. Large choices of  $\Lambda$  require more delicate cancellations between  $m_0^2(\Lambda)$  and  $\frac{y_t^2(\Lambda)}{8\pi^2}$ , while smaller values require less delicate cancellations. Thus, the delicateness of the cancellation is entirely an artifact of convention as well. In particular, the choice in (8) to set  $\Lambda$  to the physical cutoff scale  $\Lambda_{SM}$  of the Standard Model reflects an arbitrary (and not particularly convenient) choice of convention that has no bearing on the scope of the Standard Model effective field theory. The delicate cancellations can be eliminated by re-parametrizing the theory in terms of smaller values of  $\Lambda$ , which entails no loss of information or scope of the theory - at least, not from the perspective of the full, non-perturbatively defined theory. In the absence of fundamental parameters, the claim that the bare parameters  $g(\Lambda_{SM})$  at the SM's physical cutoff are more fundamental than those at lower cutoff is severely weakened, since both parametrizations describe exactly the same physics, and each can be inferred from the other. In particular, SMEFT as described by the bare parameterization  $(\tilde{m}_0^2(m_p), y_t^2(m_p))$ , where  $m_p$  is the Higgs pole mass, is no less fundamental than SMEFT as described by the bare parametrization  $(\tilde{m}_0^2(\Lambda_{SM}), y_t^2(\Lambda_{SM}))$ , even though  $\Lambda_{SM} > m_p$ .

On the view of bare parameters as conventional, regarding the delicate cancellations between  $\tilde{m}_0^2(\Lambda_{SM})$  and  $\frac{y_t^2(\Lambda_{SM})}{8\pi^2}$  as coincidence is akin to finding coincidence in the following delicate cancellations:

- We wish to determine the mass of an ant by first measuring the mass of the system (ant + X), then measuring the mass of the system (X) alone, and finally subtracting the latter from the former. Taking X=earth, we find that the mass of the system (ant + earth) agrees with the mass of the system (earth) to one part in  $10^{30}$ .
- We wish to measure the distance from the Aachen Dom (Cathedral) to the Aachen Rathaus (Town Hall). We do so by measuring the magnitude of the difference between vectors  $\hat{x}_{dom}$  and  $\hat{x}_{rat}$  describing the locations of these two buildings, where the vector components are specified relative to a coordinate system whose origin lies at the center of the Milky Way, and whose x-axis lies along the line joining the center of the Milky Way to central Aachen. We find that the x-components of  $\hat{x}_{dom}$  and  $\hat{x}_{rat}$  agree to one part in  $10^{18}$  (see Figure 1).

In both cases, the delicate agreement between the quantities in question results from an inconvenient, conventional choice of reference point, not a mysterious physical coincidence. In the first example, we might have chosen chose instead to measure the ant's mass instead by subtracting the mass of (pencil) from the mass of (ant + pencil), which would have exhibited a much less severe cancellation. The choice of reference system (pencil) or (earth) is arbitrary and conventional, while the quantity of interest - the mass of the ant - is invariant across different choices of reference system. Likewise, in the case of the Higgs, we might express the invariant Higgs pole mass as a difference between bare mass and quantum corrections defined with respect to different conventionally chosen values of  $\Lambda$ .

#### 6.5 Scientific Realism and Wilsonian EFT's

We have argued here that the validity of at least one set of naturalness-based arguments turn critically on questions of physical interpretation of effective field theories - that is, on questions concerning which elements of the mathematical formalism of an EFT may represent real features in the world, and which reflect mere choices of mathematical convention or artifacts of mathematical representation. Such questions are especially salient in the context of efforts to formulate realist interpretations of quantum field theory, which attempt to understand our theories not merely as toolkits for prediction (as operationalist or empiricist approaches tend to do), but as representing - if only in an approximate and domain-restricted way - the structure of the physical world beneath the surface of directly observable phenomena.<sup>28</sup> Within efforts to give a realist interpretation of quantum field

 $<sup>^{28}</sup>$ The difference between realist and empiricist approaches to the interpretation of scientific theories is often illustrated by reference to debates in the 19th century concerning the existence of atoms - are atoms

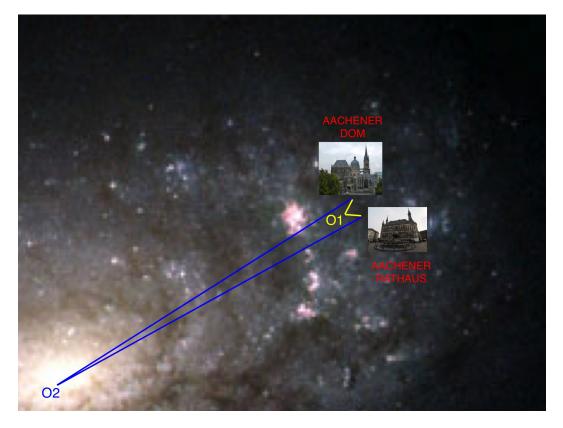


Figure 1: With choice of origin at the center of the Milky Way (O2), there is an extremely delicate cancellation - to roughly one part in  $10^{18}$  - between vectors indicating the locations of Aachen Dom (Cathedral) and Aachen Rathaus (Town Hall). However, this cancellation can be dramatically reduced by moving the origin close to, say, the midpoint between the two (O1). Likewise, the cancellation between the bare Higgs mass and its quantum corrections is very delicate for large  $\Lambda$  (say, the Planck scale), and much smaller for  $\Lambda$  on the order of the Higgs pole mass. Without fundamental parameters, the choice of the unphysical reference scale  $\Lambda$  is purely conventional and akin to a choice of origin; the delicate cancellation between bare Higgs mass and quantum corrections is then an eliminable, unphysical artifact of convention.

theory, there is the further question of which particular aspects of an EFT's formalism one should be realist *about*, given the observed empirical success of the EFT.  $^{29}$ 

Here, we wish to acknowledge one recent line of inquiry into realist interpretations of EFT's in high energy physics, and to briefly orient our own discussion with respect to the point of view considered in this work. Williams, J. Fraser, and Ruetsche have recently explored the notion that the renormalization group may be used as a guide in attempting to uncover which mathematical features of empirically successful EFT's to regard as representing real features in the world, which are likely to be preserved in future, more fundamental theories. Invoking Wimsatt's criterion of robustness for realist commitment, Williams writes, "What the RG shows is that the 'fundamental' short-distance structure ... is largely irrelevant to the physical content of an EFT in the domain where we have any reason to consider it empirically reliable ... An EFT at long distances is 'robust' in a way that the short distance 'fundamental' theory is demonstrably not: its entities and structures at that scale are 'accessible (detectable, measurable, derivable, definable, producible, or the like) in a variety of independent ways,' and so are candidates for being included in the ontology of that EFT" (Williams, 2017), (Wimsatt, 2007). In a similar vein, Fraser writes, "in demonstrating that the large scale properties of a QFT model are insensitive to the high energy dynamics, the renormalisation group is also telling us that these properties are essentially independent of the details of future physical theories which describe the dynamics of currently inaccessible high energy degrees of freedom. Thus the renormalisation group gives us a way of identifying properties of our present theories which will be embedded within future theories, in one way or another" (Fraser, 2016). Thus, both Fraser and Williams see the RG as facilitating the interpretation of EFT's by identifying those low-energy features that are robust against variations in the unknown high-energy physics, and therefore likely to be preserved irrespective of what this new physics turns out to be.

On the other hand, Ruetsche writes that the arguments offered by Williams and Fraser in support of this view are "compromised by a certain faux generality afflicting RG analyses." She explains, "The concern is that even explicit RG results are only as reassuring as the space of theories on which the RG group acts is comprehensive. But that space incorporates assumptions about what kinds of interactions are possible and how to model them. And nature isn't beholden to respect those assumptions" (Ruetsche, Forthcoming 2018). In particular, proofs based on the RG that many distinct theories with different values of irrelevant operator coefficients are well approximated at low energies by the same renormalizable theory assume that both the fundamental high-energy theory and approximate low-energy theory reside in the same parameter space describing the same set of fields. On the other hand, Ruetsche suggests, the space of possible high-energy theories may extend even beyond the realm of quantum field theory, and so is much larger than the set of possibilities represented by the parameter space that hosts the Wilsonian RG flow.

The interpretation of Wilsonian EFT's without fundamental parameters, which restricts realist commitment to Wilsonian RG invariants, is motivated by many of the considerations that drive the realism of Williams and Fraser; however, there are several important distinctions that we wish to draw here between the particular realist approach to interpreting

fictitious theoretical constructs that are merely useful for describing the observable behavior of gases and other physical systems, or do they really exist? The empiricist or instrumentalist view of atoms (which has declined markedly in popularity) adopts the first view, while the realist view adopts the latter. For more detailed analysis of this debate, see for example Psillos' (Psillos, 2011).

<sup>&</sup>lt;sup>29</sup>Efforts to interpret effective field theories, and quantum field theories generally, from an empiricist point of view can be found, for example, in Butterfield and Bouatta's (Butterfield and Bouatta, 2015), Ruetsche's (Ruetsche, 2011), Fraser's (Fraser, 2011), and Halvorson and Müger's (Halvorson, 2013).

QFT's that is advocated by these authors and the brand of realism that informs the view of EFT's sketched in this section. We agree with Williams and Fraser, that in the physical interpretation of EFT's, one must take care to distinguish between those aspects of an EFT's formalism that play a central role in generating its successful empirical predictions and those that do not. <sup>30</sup> As we have seen, it is precisely such considerations that motivate the abandonment of fundamental parameters in the physical interpretation of Wilsonian EFT's, since the notion that there exists a single physically preferred parametrization of the theory at its physical cutoff plays no essential role in generating the theory's successful predictions (or in making it mathematically well-defined). <sup>31</sup>

However, the precise sense in which Williams and Fraser use the Wilsonian RG to identify candidates for realist commitment differs from the sense in which the interpretation of Wilsonian EFT's sketched in this section does so. As discussed, Williams and Fraser use the Wilsonian RG to identify elements of an EFT that are robust to changes in the specification of a theory at large values of the parameter  $\Lambda$  (typically, near the physical cutoff): since we are ignorant as to the true nature of physics near the physical cutoff (at least, in the case of the Standard Model effective field theory) we should restrict our realism to quantities that do not depend on these details.

We agree with this claim, and simply wish to note that there is a distinct and compatible sense in which the Wilsonian RG may be used to identify candidates for realist commitment in EFT's. By restricting physical quantities in an EFT to Wilsonian RG invariants, the physical interpretation of EFT's sketched in this section ventures a hypothesis about the semantic relationship between an EFT and the physical world, rather than a claim about our *epistemic* relationship to the world. For example, given that there is some matter of fact - albeit currently unknown to us - about the values of the irrelevant operator coefficients that describe physics near the Standard Model's physical cutoff scale, what features of that non-renormalizable EFT's mathematical formalism represent real features in the world, and which are mere artifacts of representation? One possibility is that there really exist fundamental bare parameters that can in principle be directly measured (by analogy with the microscopic parameters of a condensed matter system). Another possibility is that the bare cutoff parameters of that EFT do not represent real features in the world, and instead merely reflect an arbitrary choice of parametrization of physical amplitudes, akin to a choice of gauge or coordinate system. As we have argued, the historical progression of EFT's to ever-higher energies appears to support the latter view: in the case of the non-renormalizable 4-Fermi theory of weak interactions, we possess empirical access to physics near and beyond the physical cutoff, but do not measure the bare cutoff parameters of this EFT directly; there does not appear to be any empirical evidence for the notion that there are genuine physical facts about the values of the bare parameters, even in cases where we can probe physics near the cutoff. Things could be different in the case of Standard Model effective field theory, since we do not yet have access to physics near its cutoff; however, there does

<sup>&</sup>lt;sup>30</sup>This strategy constitutes a central component of what Psillos has labeled the "divide and conquer" approach to scientific realism. (Psillos, 2005). For a closely related approach to the realist interpretation of quantum theories in general, see Saatsi (Saatsi, 2017).

<sup>&</sup>lt;sup>31</sup>The situation is partly analogous to the distinction between the mechanical theory of Lorentz, which predicted relativistic effects such as time dilation, length contraction, and the like, assuming a physically preferred frame of reference, and the relativity of Einstein, which recovered the same effects but relinquished the idle assumption of a preferred frame. Until it is possible to independently measure the bare parameters of an EFT (rather than working backwards from correlation functions), the notion of fundamental parameters appears to rest primarily on metaphysical speculation motivated by analogies with condensed matter physics, much as intuitions motivating the introduction of an ether in the 19th century rested in part on metaphysical speculation motivated by analogies with the mechanical theory of elastic media.

not appear to much by way of empirical evidence that this is the case, either. Thus, while the realism of Williams and Fraser appears to be consistent with (if not explicitly to endorse) the physical interpretation of Wilsonian EFT's in terms of fundamental parameters, the interpretation sketched in this section explicitly rejects this possibility on the grounds that these quantities are not invariant under Wilsonian RG transformations.

### 7 Conclusion

One influential rationale for imposing naturalness is based on the notion of "fundamental parameters." We have argued that it is possible to abandon this notion in the mathematical definition of Wilsonian EFT's without sacrificing predictive power or the virtue of finiteness introduced by the Wilsonian approach. On the other hand, one way of understanding Wilsonian EFT's in the absence of fundamental parameters also invites abandonment of several other traditional dogmas of Wilsonian effective field theory. From this alternative point view, it becomes possible to understand the delicate cancellation between Higgs bare mass and quantum corrections as an eliminable artifact resulting from a particular choice of mathematical convention, and the problem of explaining these cancellations seems much less urgent, if not wholly misguided. On the other hand, this way of understanding Wilsonian EFT's without fundamental parameters does nothing to undermine the expectation that the Standard Model as a whole should be embedded in a deeper theory that includes gravity, which should explain why Standard Model effective field theory is characterized by the particular RG trajectories that it is. Rather, it only weakens the case that there is an especially urgent need for explanation attached to the Higgs mass but not other SM parameters.

Of course, there also exist other formulations of the naturalness principle that we have not considered here, such as fine tuning formulations based on matching between EFT's in the  $\overline{MS}$  scheme, and formulations based on the notion of inter-scale autonomy, each of which needs to be examined in detail. We think it likely that similar concerns to those that arise in the context of Higgs bare mass fine tuning will arise in the context of these other formulations, as well as in the cosmological constant problem. However, in each of these instances, a rigorous case remains to be made.

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#### References

- Greg W Anderson and Diego J Castano. Measures of fine tuning. Physics Letters B, 347 (3-4):300–308, 1995.
- Jonathan Bain. Emergence in effective field theories. European journal for philosophy of science, 3(3):257–273, 2013.

- Riccardo Barbieri and Gian Francesco Giudice. Upper bounds on supersymmetric particle masses. Nuclear Physics B, 306(1):63–76, 1988.
- Jürgen Berges, Nikolaos Tetradis, and Christof Wetterich. Non-perturbative renormalization flow in quantum field theory and statistical physics. *Physics Reports*, 363(4):223–386, 2002.
- Eugenio Bianchi and Carlo Rovelli. Why all these prejudices against a constant? arXiv preprint arXiv:1002.3966, 2010.
- J. Butterfield. Emergence, reduction and supervenience: a varied landscape. Foundations of Physics, 41(6):920–959, 2011a.
- Jeremy Butterfield. Less is different: emergence and reduction reconciled. *Foundations of Physics*, 41(6):1065–1135, 2011b.
- Jeremy Butterfield. Reduction, emergence, and renormalization. *The Journal of Philosophy*, 111(1):5–49, 2014.
- Jeremy Butterfield and Nazim Bouatta. Emergence and reduction combined in phase transitions. In *FRONTIERS OF FUNDAMENTAL PHYSICS: The Eleventh International Symposium*, volume 1446, pages 383–403. AIP Publishing, 2012.
- Jeremy Butterfield and Nazim Bouatta. Renormalization for philosophers. Metaphysics in Contemporary Physics, 104:437–485, 2015.
- Elena Castellani. Reductionism, emergence, and effective field theories. Studies in History and Philosophy of Science Part B: Studies in History and Philosophy of Modern Physics, 33(2):251–267, 2002.
- John C Collins. Renormalization: an introduction to renormalization, the renormalization group and the operator-product expansion. Cambridge university press, 1984.
- Karen Crowther. Decoupling emergence and reduction in physics. European Journal for Philosophy of Science, 5(3):419–445, 2015.
- Karen Crowther. Inter-theory relations in quantum gravity: Correspondence, reduction, and emergence. arXiv preprint arXiv:1712.00473, 2017.
- Bertrand Delamotte. An introduction to the nonperturbative renormalization group. In Renormalization Group and Effective Field Theory Approaches to Many-Body Systems, pages 49–132. Springer, 2012.
- Samuel C Fletcher. Similarity, topology, and physical significance in relativity theory. *The* British Journal for the Philosophy of Science, 67(2):365–389, 2015.
- Alexander Franklin. Whence the effectiveness of effective field theories? 2017.
- Doreen Fraser. Quantum field theory: Underdetermination, inconsistency, and idealization. *Philosophy of Science*, 76(4):536–567, 2009.
- Doreen Fraser. How to take particle physics seriously: A further defence of axiomatic quantum field theory. Studies In History and Philosophy of Science Part B: Studies In History and Philosophy of Modern Physics, 42(2):126–135, 2011.

- Doreen Fraser. The development of renormalization group methods for particle physics: Formal analogies between classical statistical mechanics and quantum field theory. *Preprint: http://philsci-archive.pitt.edu/14591/*, 2018.
- Doreen Fraser and Adam Koberinski. The higgs mechanism and superconductivity: A case study of formal analogies. *Studies in History and Philosophy of Science Part B: Studies in History and Philosophy of Modern Physics*, 55:72–91, 2016.
- James Duncan Fraser. What is Quantum Field Theory? Idealisation, Explanation and Realism in High Energy Physics. PhD thesis, University of Leeds, 2016.
- James Duncan Fraser. The real problem with perturbative quantum field theory. *The British Journal for the Philosophy of Science*, 2017.
- Simon Friederich, Robert Harlander, and Koray Karaca. Philosophical perspectives on ad hoc hypotheses and the higgs mechanism. Synthese, 191(16):3897–3917, 2014.
- Gian F Giudice. Naturalness after lhc8. arXiv preprint arXiv:1307.7879, 2013.
- Gian Francesco Giudice. The dawn of the post-naturalness era. arXiv preprint arXiv:1710.07663, 2017.
- H. Halvorson. The semantic view, if plausible, is syntactic. *Philosophy of Science*, 80(3), 2013.
- Leif Hancox-Li. Solutions in constructive field theory. *Philosophy of Science*, 84(2):335–358, 2017.
- Stephan Hartmann. Effective field theories, reductionism and scientific explanation. Studies in History and Philosophy of Science Part B: Studies in History and Philosophy of Modern Physics, 32(2):267–304, 2001.
- S Hossenfelder. Screams for explanation: Finetuning and naturalness in the foundations of physics. arXiv preprint arXiv:1801.02176, 2018.
- Sabine Hossenfelder. Naturalness: Or how religion turned to math. URL https://www. youtube.com/watch?v=w7VJQof8hhY.
- Nick Huggett and Robert Weingard. The renormalisation group and effective field theories. Synthese, 102(1):171–194, 1995.
- Charles Kittel, Paul McEuen, and Paul McEuen. Introduction to solid state physics, volume 8. Wiley New York, 1996.
- Stephen P Martin. A supersymmetry primer. In *Perspectives on supersymmetry II*, pages 1–153. World Scientific, 2010.
- Michael Miller. Mathematical structure and empirical content. http://philsciarchive.pitt.edu/12678/, 2016.
- István Montvay and Gernot Münster. *Quantum fields on a lattice*. Cambridge University Press, 1997.

- Tim R Morris. The exact renormalization group and approximate solutions. International Journal of Modern Physics A, 9(14):2411–2449, 1994.
- Tim R Morris. Elements of the continuous renormalization group. *Progress of Theoretical Physics Supplement*, 131:395–414, 1998.
- M.E. Peskin and D.V. Schroeder. An Introduction to Quantum Field Theory. 1996.
- Joseph Polchinski. Renormalization and effective lagrangians. *Nuclear Physics B*, 231(2): 269–295, 1984.
- Stathis Psillos. Scientific realism: How science tracks truth. Routledge, 2005.
- Stathis Psillos. Moving molecules above the scientific horizon: On perrin's case for realism. Journal for General Philosophy of Science, 42(2):339–363, 2011.
- Vincent Rivasseau. From perturbative to constructive renormalization. Princeton University Press, 2014.
- Joshua Rosaler. Inter-theory Relations in Physics: Case Studies from Quantum Mechanics and Quantum Field Theory. PhD thesis, University of Oxford, 2013.
- Joshua Rosaler. Local reduction in physics. Studies in History and Philosophy of Science Part B: Studies in History and Philosophy of Modern Physics, 50:54–69, 2015.
- Joshua Rosaler. Reduction as an a posteriori relation. The British Journal for the Philosophy of Science, 2017.
- Oliver J Rosten. Fundamentals of the exact renormalization group. *Physics Reports*, 511 (4):177–272, 2012.
- Laura Ruetsche. Interpreting quantum theories. Oxford University Press, 2011.
- Laura Ruetsche. *Renormalization Group Realism: The Assent of Pessimism*, volume Scientific Realism and the Quantum. Oxford University Press, Forthcoming 2018.
- Juha Saatsi. Scientific realism meets metaphysics of quantum mechanics. http://philsciarchive.pitt.edu/14583/, 2017.
- Matthew D Schwartz. *Quantum field theory and the standard model*. Cambridge University Press, 2014.
- Witold Skiba. Tasi lectures on effective field theory and precision electroweak measurements. arXiv preprint arXiv:1006.2142, 2010.
- Mark Srednicki. Quantum field theory. Cambridge University Press, 2007.
- Raymond F Streater and Arthur S Wightman. *PCT*, spin and statistics, and all that. Princeton University Press, 2016.
- Leonard Susskind. Dynamics of spontaneous symmetry breaking in the weinberg-salam theory. *Physical Review D*, 20(10):2619, 1979.

- Gerard 't Hooft. Naturalness, chiral symmetry, and spontaneous chiral symmetry breaking. Recent developments in gauge theories. Proceedings of the NATO Advanced Study Institute on recent developments in gauge theories, held in Cargèse, Corsica, August 26-September 8, 1979, pages 135–157, 1980.
- D. Wallace. In defence of naivete: The conceptual status of Lagrangian quantum field theory. Synthese, 151:33–80, 2006.
- David Wallace. Taking particle physics seriously: A critique of the algebraic approach to quantum field theory. *Studies in History and Philosophy of Science Part B: Studies in History and Philosophy of Modern Physics*, 42(2):116–125, 2011.
- James D Wells. The utility of naturalness, and how its application to quantum electrodynamics envisages the standard model and higgs boson. *Studies in History and Philosophy* of Science Part B: Studies in History and Philosophy of Modern Physics, 49:102–108, 2015.
- C Wetterich. Fine-tuning problem and the renormalization group. *Physics Letters B*, 140 (3-4):215–222, 1984.
- C Wetterich. Where to look for solving the gauge hierarchy problem? *Physics Letters B*, 718(2):573–576, 2012.
- Christof Wetterich. Average action and the renormalization group equations. Nuclear Physics B, 352(3):529–584, 1991.
- Christof Wetterich. Exact evolution equation for the effective potential. *Physics Letters B*, 301(1):90–94, 1993.
- Porter Williams. Naturalness, the autonomy of scales, and the 125gev higgs. Studies in History and Philosophy of Science Part B: Studies in History and Philosophy of Modern Physics, 51:82–96, 2015.
- Porter Williams. Scientific realism made effective. The British Journal for the Philosophy of Science, 2017.
- William C Wimsatt. Re-engineering philosophy for limited beings: Piecewise approximations to reality. Harvard University Press, 2007.
- Peter Woit. What scientific idea is ready for retirement? the "naturalness" argument. 2014. URL https://www.edge.org/response-detail/25416.